

Lecture 11, 18.03.2020

Tracking detectors

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Particle Physics Experiments

Accelerate a beam of (stable & charged) particles to high energies

→ electrons/positrons, protons/antiprotons, heavy ions

Bring them into collision with

another beam of particles:

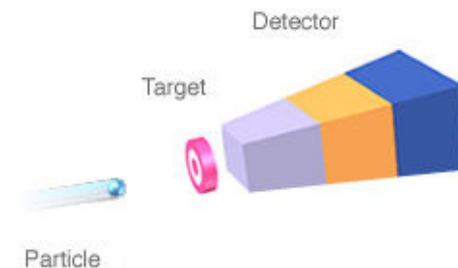
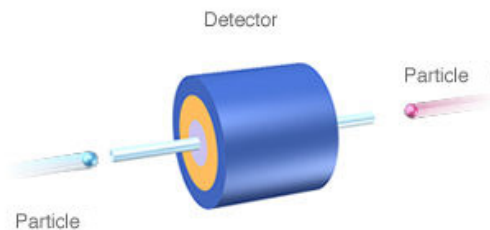
“collider experiment”

e.g. ATLAS, CMS

a target at rest:

“fixed-target experiment”

e.g. SHiP



Measure the properties of the long-lived particles
that are created in the collision

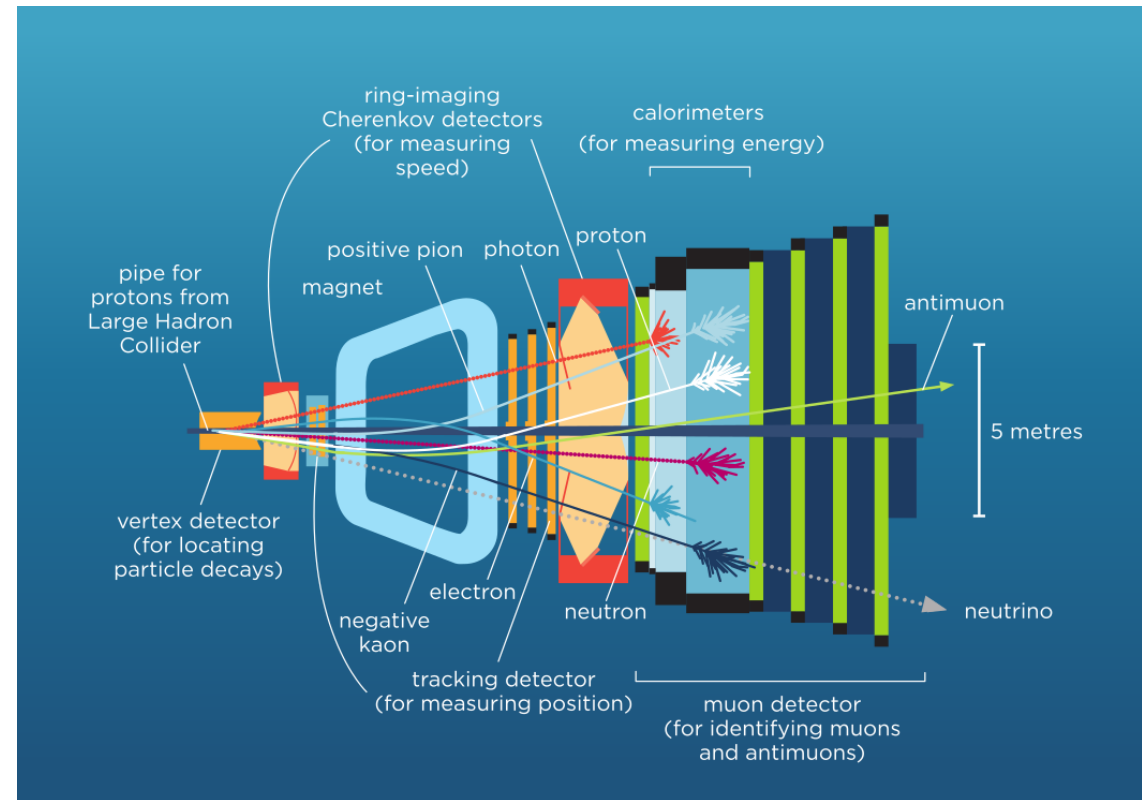
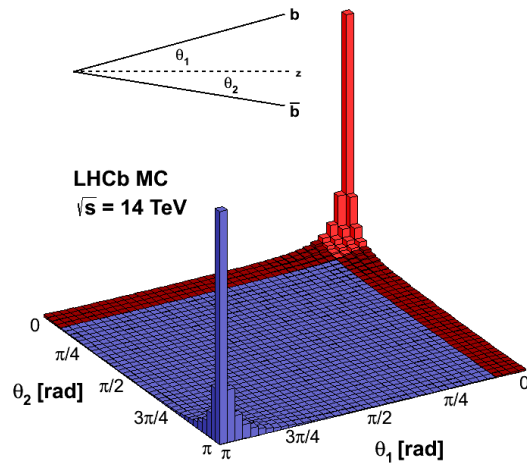
Reconstruct short-lived particles using relativistic kinematics

LHCb Experiment

A collider experiment that looks like a fixed target experiment

Main goal is to study *b* and *c* hadrons

→ are produced mostly at small angles wrt beam axis



Detector Components

Position-sensitive detectors

- production vertices and flight path of charged particles
 - decay vertices of short-lived particles

Position sensitive detectors in a magnetic field

- momenta of charged particles

Calorimeters

- energy of charged and neutral particles

Cherenkov counters, Transition radiation counters, Time-of-flight counters, ...

- speed of charged particles
(momentum + speed → mass → particle type)

Momentum measurement

Moving charge in magnetic field → Lorentz force

$$\vec{F}_L = q \cdot \vec{v} \times \vec{B}$$

→ forces particle onto circular trajectory around field lines

$$\frac{m \cdot v^2}{r} = q \cdot v \cdot B$$

$$p = q \cdot B \cdot r$$

→ measure bending radius of particle trajectory
in a known magnetic field

→ for a particle with $q = \pm e$

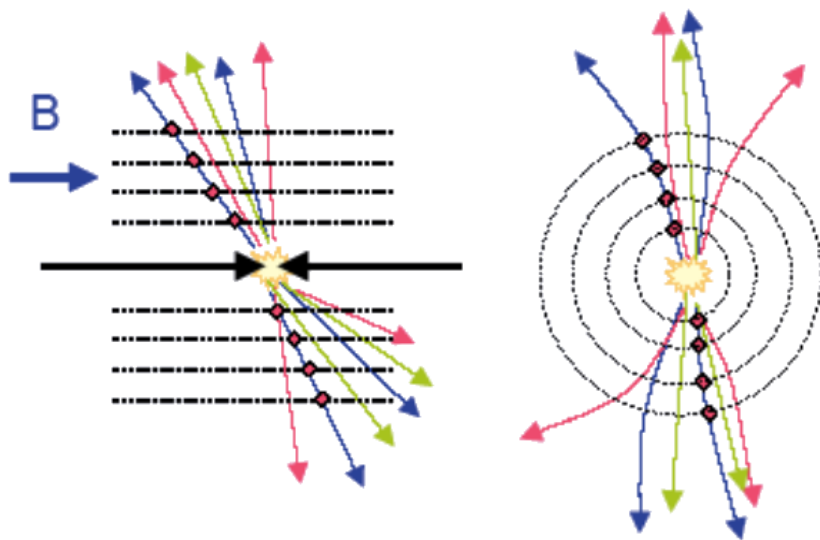
$$p [\text{GeV}] \approx 0.3 \cdot B [\text{T}] \cdot r [\text{m}]$$

Momentum measurement

**Typical collider experiment:
solenoid or toroid magnet**

→ field lines parallel to beam

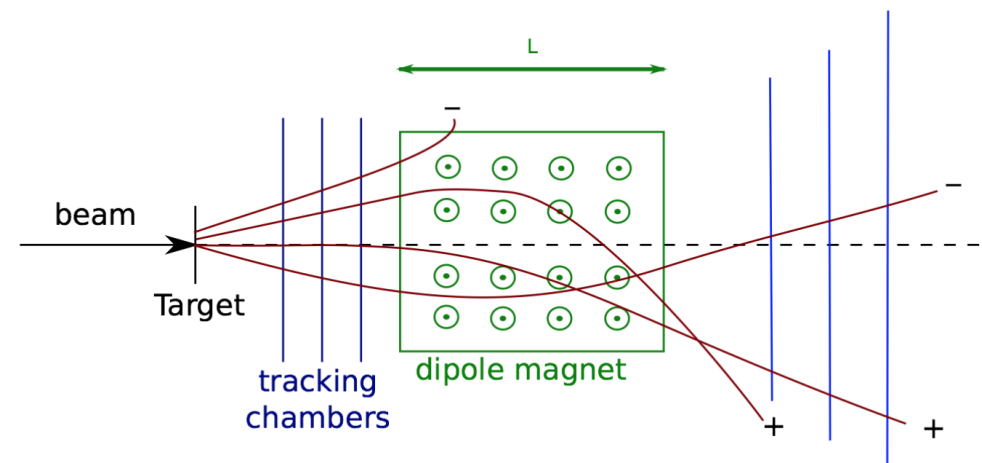
**cylindrical tracking layers
inside the magnet**



**Typical fixed-target experiment:
dipole magnet**

→ field lines orthogonal to beam

**planar tracking detectors
before and after the magnet**



Momentum resolution (I)

“Gluckstern equation” for N equidistant measurements:

$$\frac{\sigma(p)}{p} = \sqrt{\frac{720}{N+4}} \cdot \sigma_x \cdot \frac{p}{0.3 B L^2}$$

Relative momentum resolution

- degrades linearly with increasing momentum
- improves linearly with spatial resolution of the detector
- improves linearly with the strength of the magnetic field
 - improves **quadratically** with the length of the measured track segment

Main reason for the large size of high-energy physics experiments

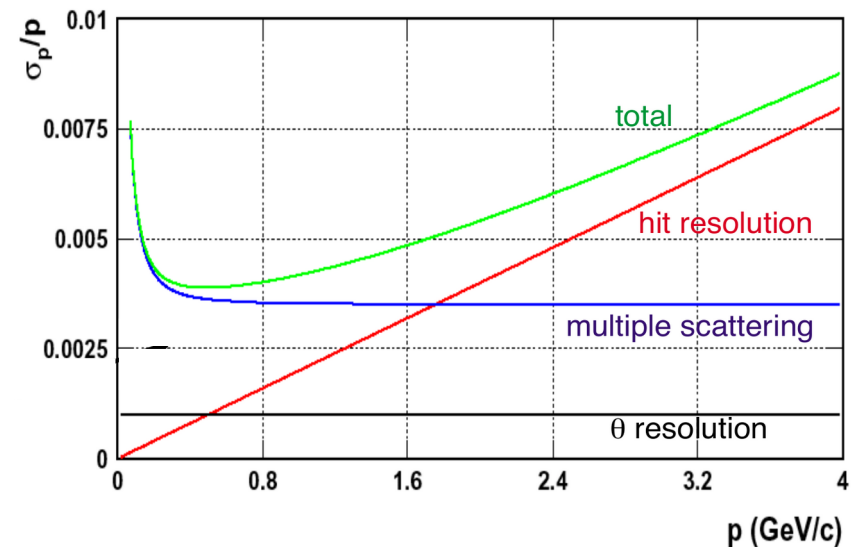
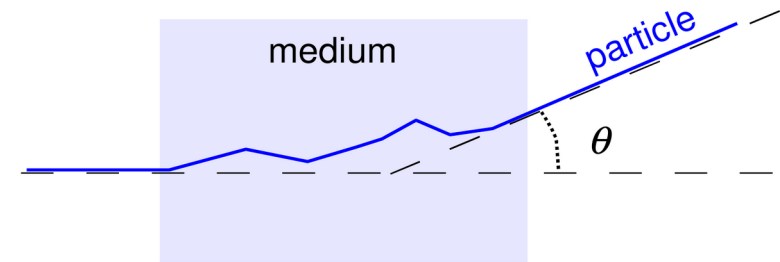
Momentum resolution (II)

Particle trajectory disturbed due to multiple scattering in the material of the detector

Causes deterioration of momentum resolution

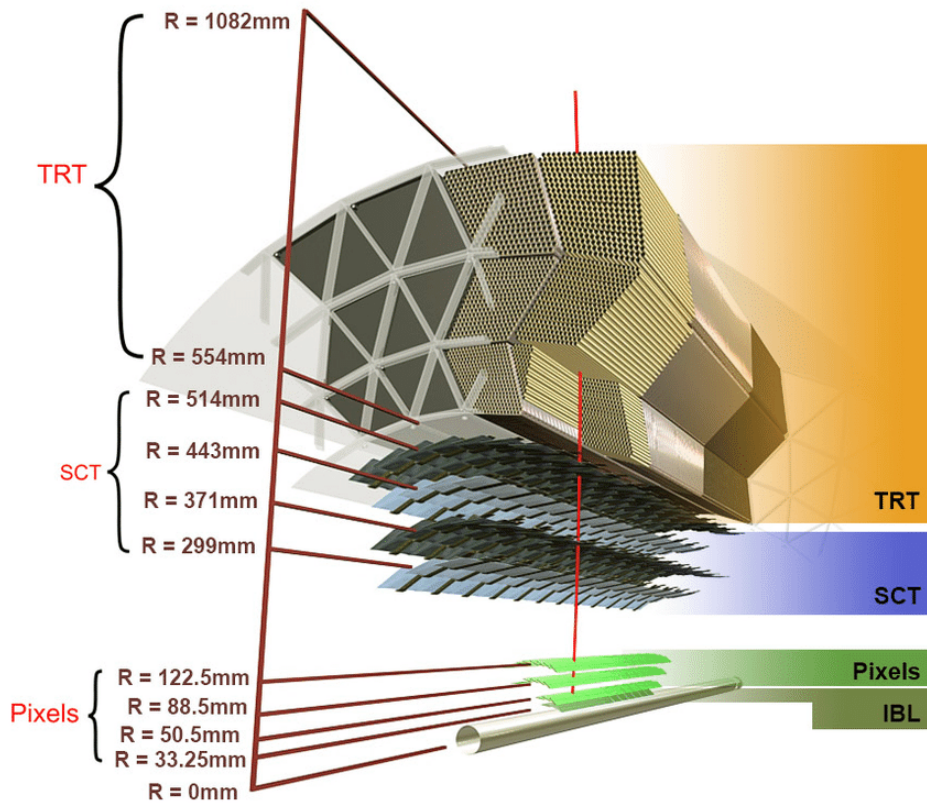
$$\frac{\sigma(p)}{p} = \frac{0.2 \cdot \sqrt{L/X_0}}{\beta \cdot B \cdot L}$$

- limits momentum resolution at low momenta (small β)
- material often dominated by supports, cables, etc (“dead material”)

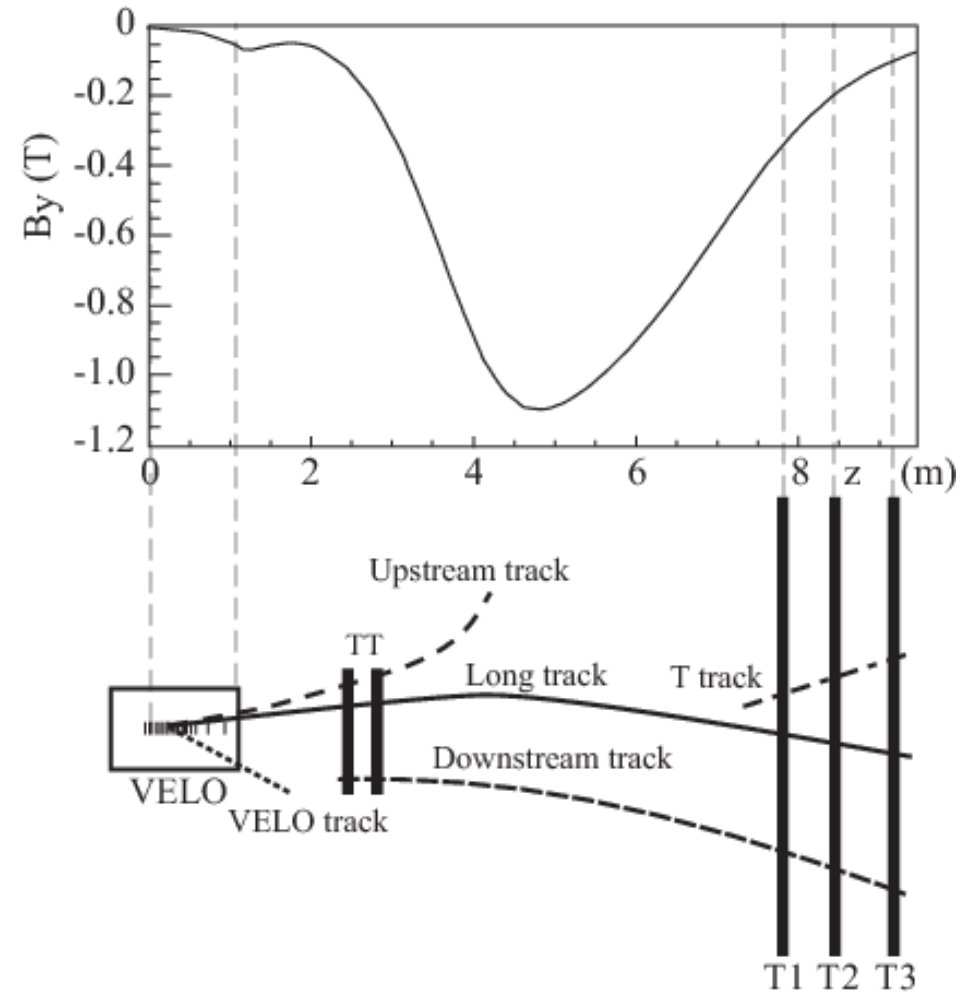


Momentum resolution (III)

ATLAS tracking system

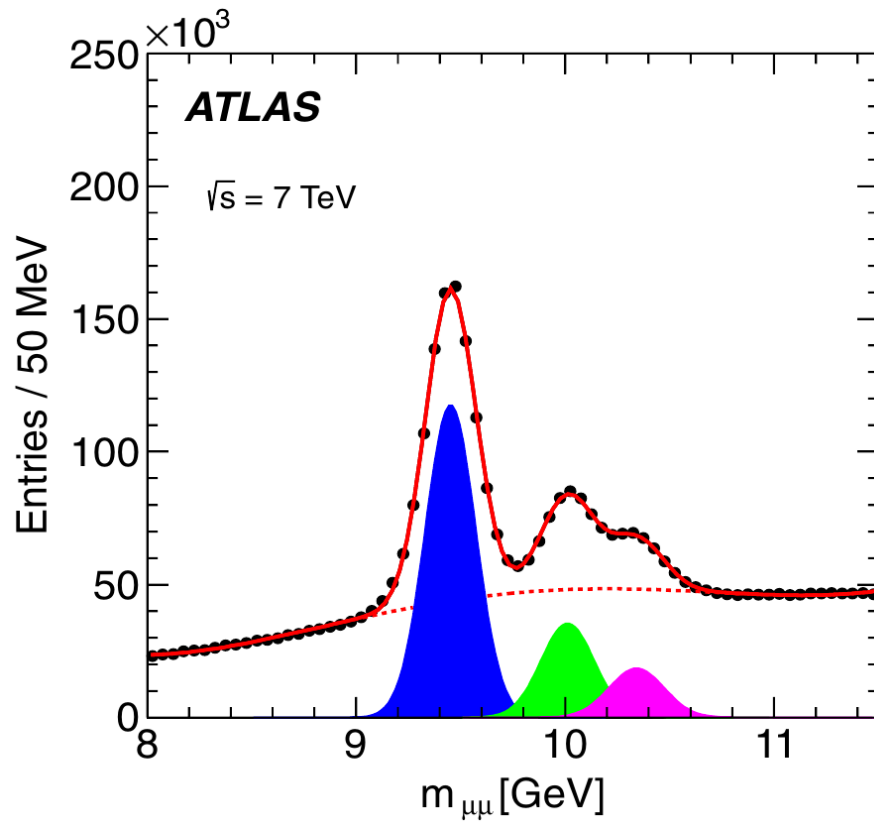


LHCb tracking system

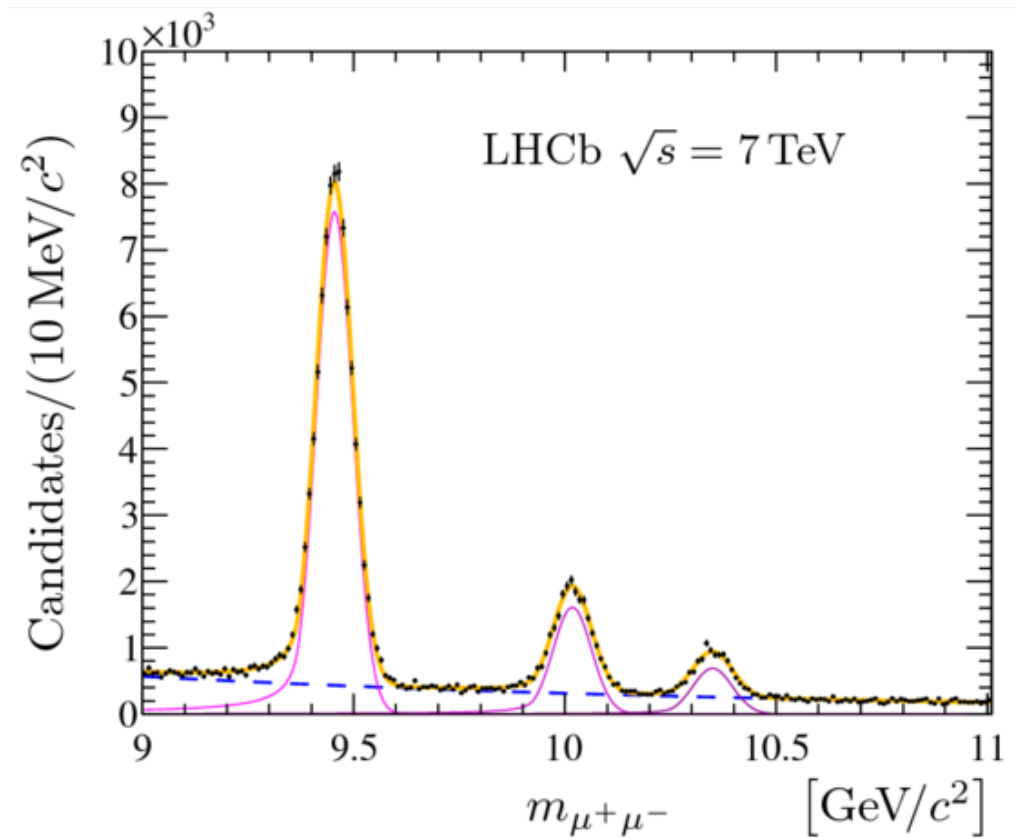


Momentum resolution (IV)

Υ resonances in ATLAS



Υ resonances in LHCb



[PRD87(2013)052004]

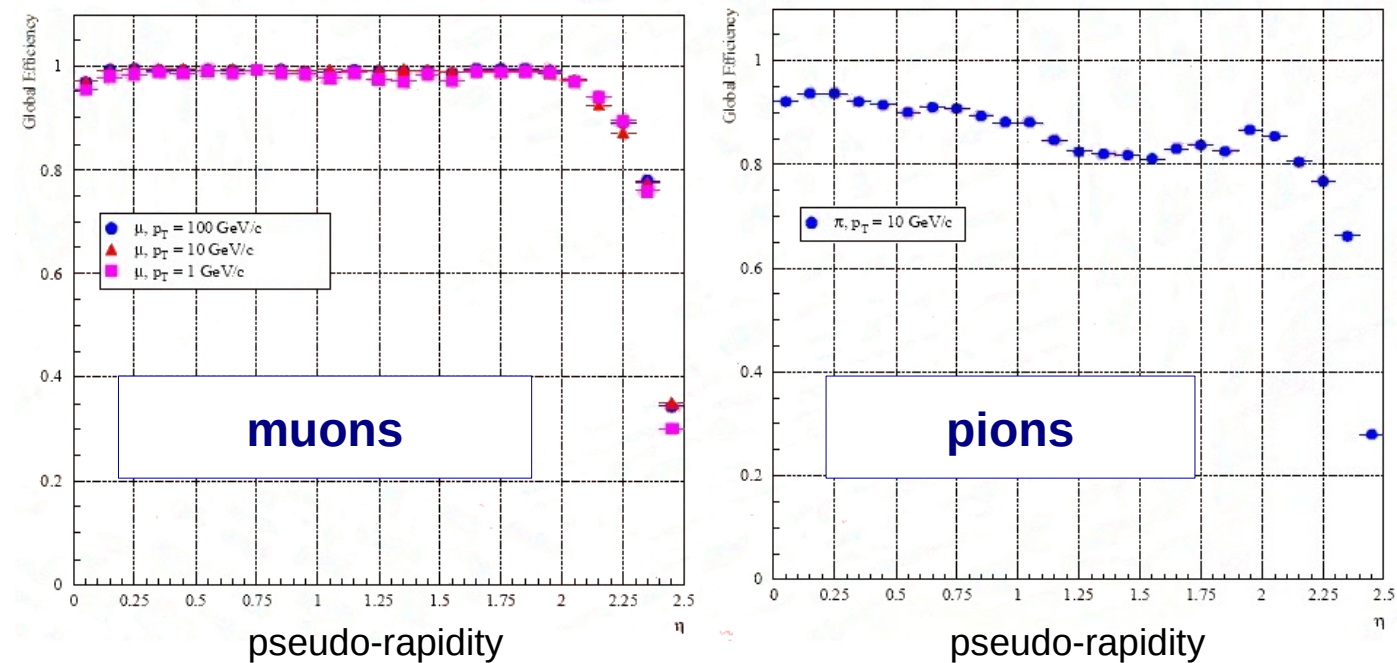
[JHEP(2015)103]

Hadronic Interactions

Hadrons also undergo nuclear interactions in detector material

- large kink in trajectory or shower of secondary particles
- loss in reconstruction efficiency

Example CMS:

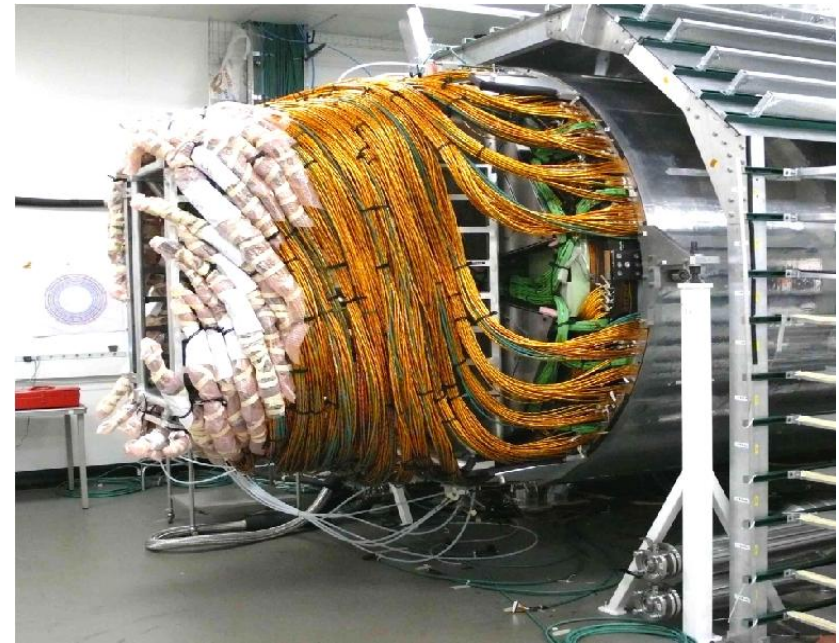
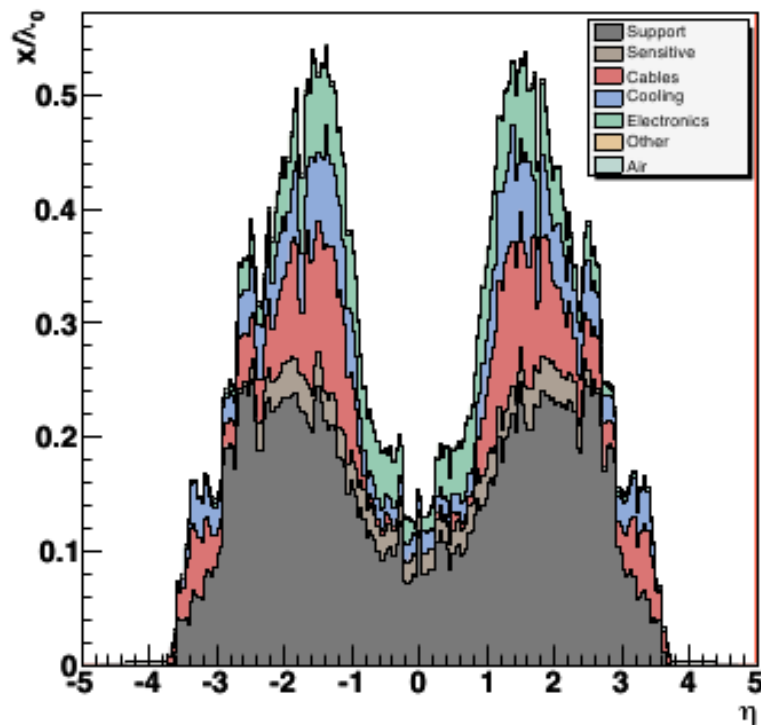


Hadronic Interactions

Hadrons also undergo nuclear interactions in detector material

- large kink in trajectory or shower of secondary particles
- loss in reconstruction efficiency

Example CMS:



Requirements

Spatial hit resolution

→ vertex resolution, momentum resolution, ...

Granularity

→ ability to separate two particles that pass the detector close in space

Rate capability

→ ability to separate two particles that pass the detector close in time

Material budget

→ minimize multiple scattering, hadronic interactions

Radiation hardness

→ performance degradation from degradation of detector material

Cost !!!

→ often dominated by readout electronics

(number of channels, amount of information per channel)

Requirements

Close to interaction point: highest particle density ...

→ need fine granularity, excellent position resolution,
radiation hardness

... but small tracking volume

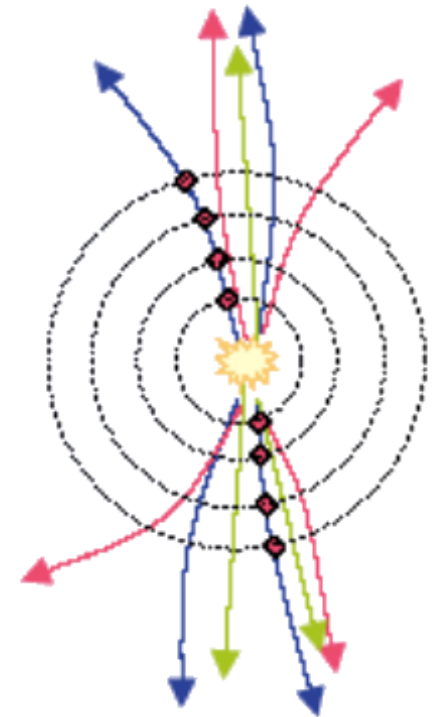
→ can afford expensive detectors with
fine granularity, many readout channels

Further away: large tracking volume ...

→ need cost effective detector

... but lower particle density

→ can afford coarser granularity, lower position resolution



Early tracking detectors

E.g. cloud chamber (Wilson, 1912):

Vessel filled with supersaturated water vapour

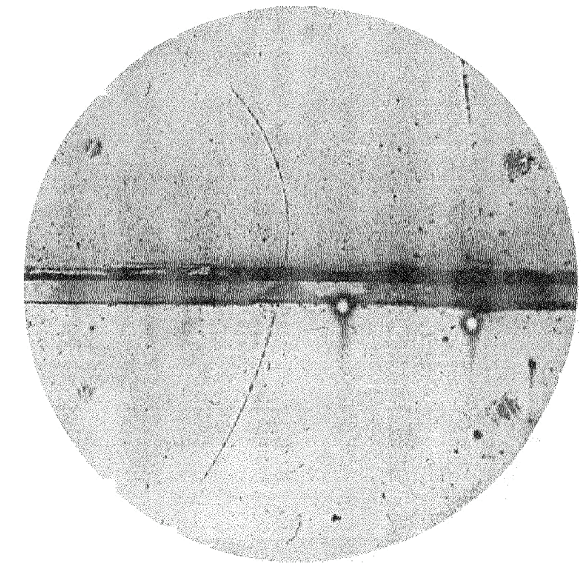
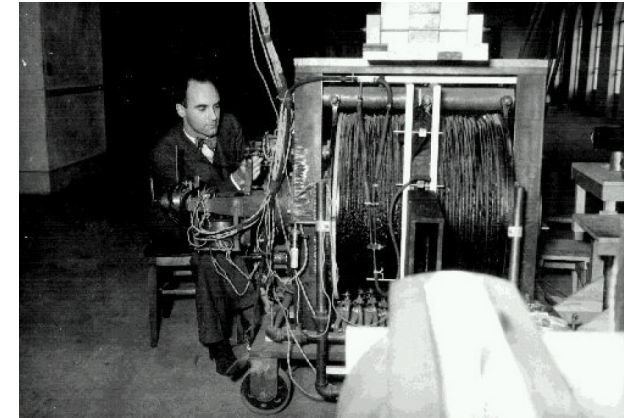
- charged particle creates ionisation clusters
- ionisation clusters act as condensation nuclei
- trail of water droplets along particle trajectory

Photograph trails through windows in the vessel

- spatial resolution $\sim 100 \mu\text{m}$
- estimate particle energy from density of droplets

Most important experimental tool until 1950s, but

- low rate capability
- tedious manual analysis of photographs



discovery of positron
(Anderson, 1932)

Modern tracking detectors

Charged particle interacts with detector material

→ creates free charge carriers (e.g. by ionization)

Apply electric field across detector volume

→ collect charges on segmented electrodes

Electronically amplify & shape signal pulse

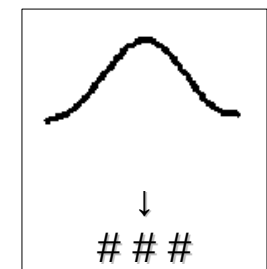
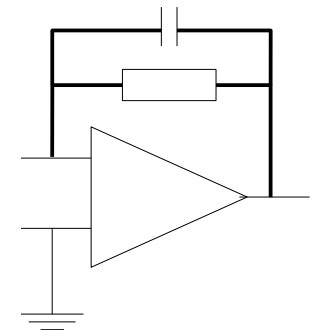
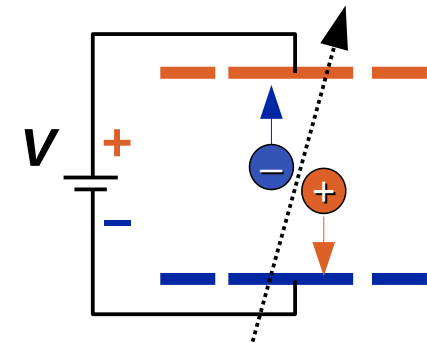
Digitize the signal

→ discriminator: hit / no hit

→ ADC: encode pulse height

→ TDC: encode signal arrival time

**Transfer digital data to a computer farm
for processing and storage**



Gaseous tracking detectors

Cylindrical tube, filled with gas mixture,
thin wire strung along its centre

High voltage (typically 1–2 kV)
between wire and outer wall

Charged particle ionizes gas atoms

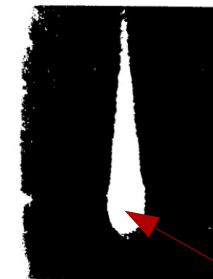
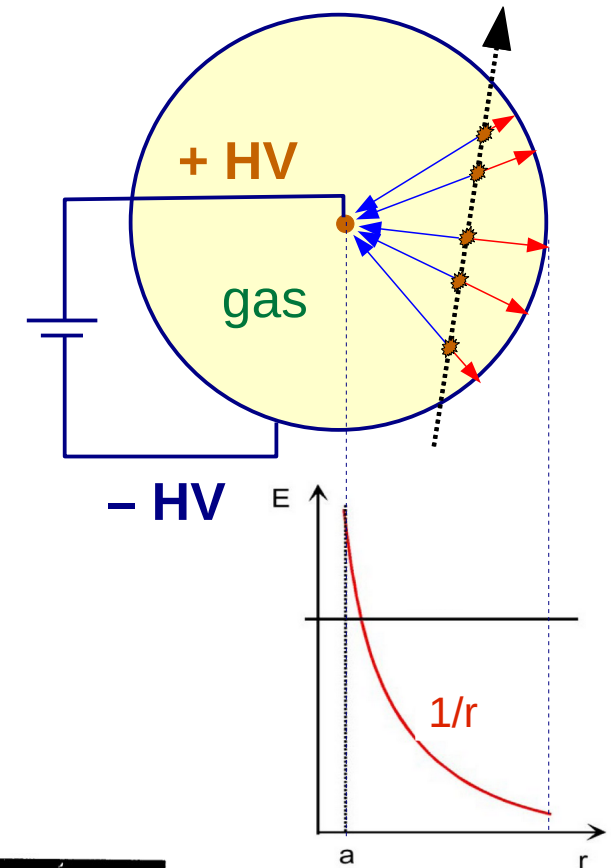
→ electrons drift towards the wire

Very high electric field close to the wire

→ electrons gain enough energy
to ionize secondary atoms

→ charge avalanche

→ measurable voltage pulse on wire

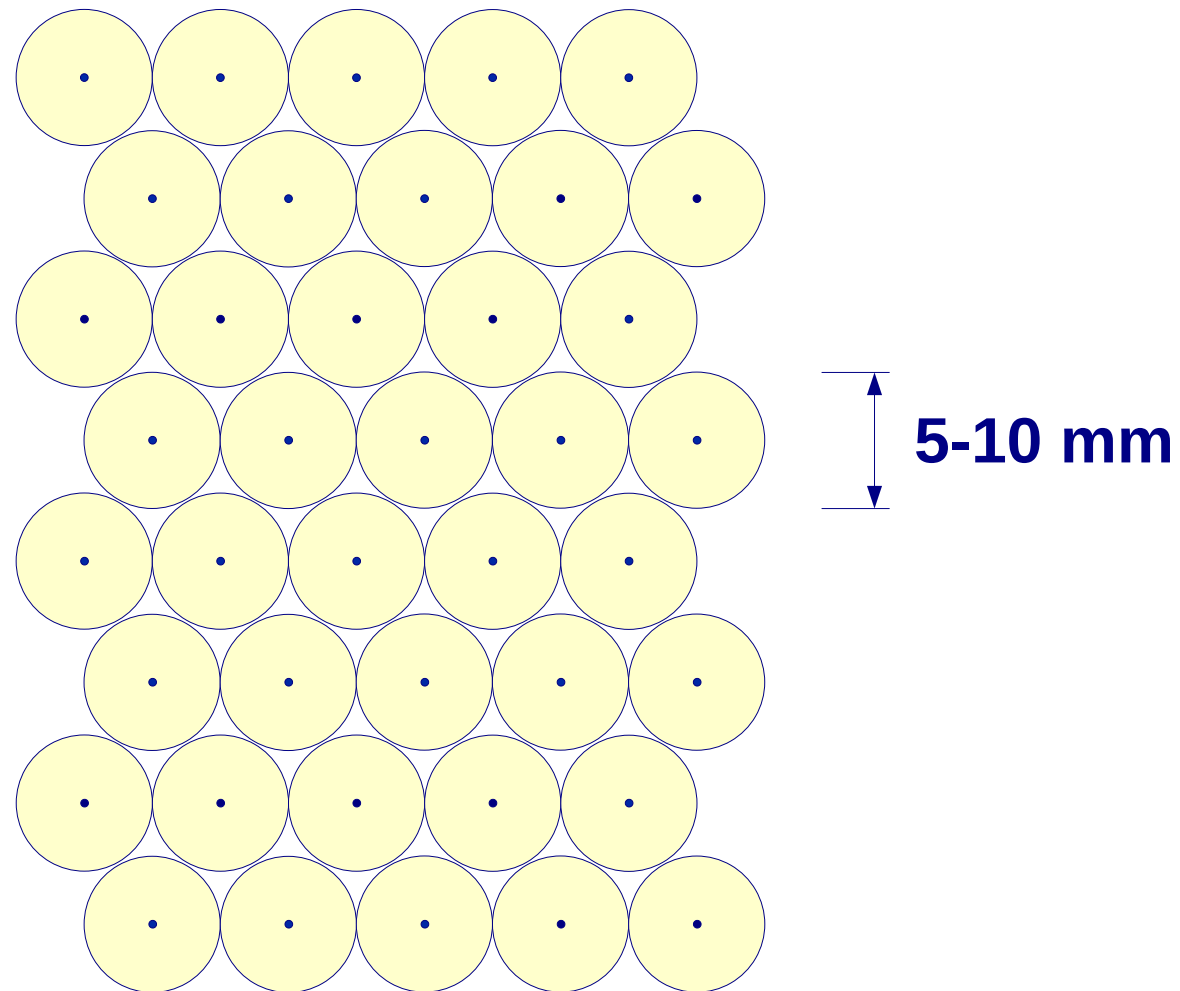


photograph of a
charge avalanche

wire

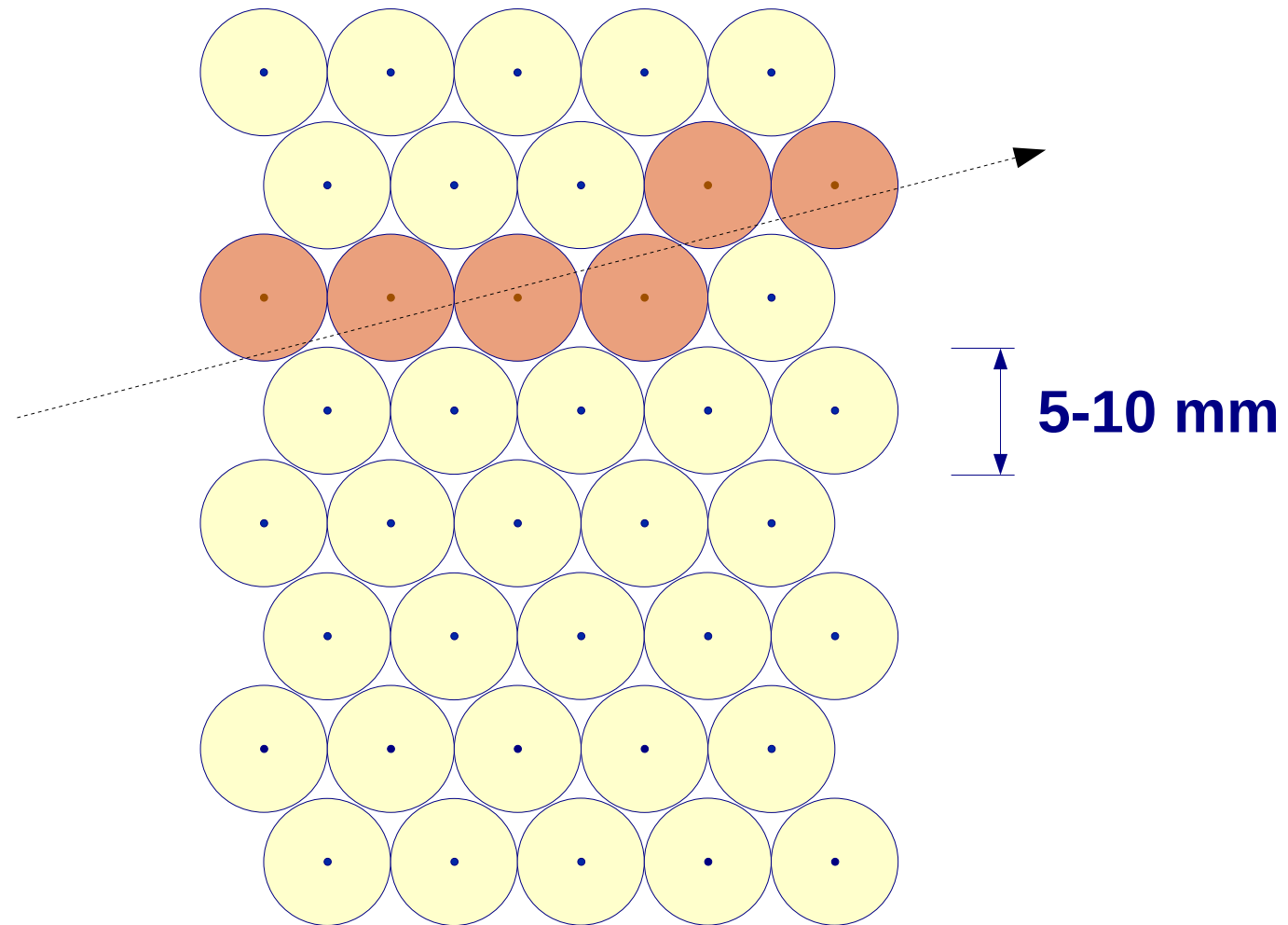
Gaseous tracking detectors

Tracking detector: several layers of such drift tubes



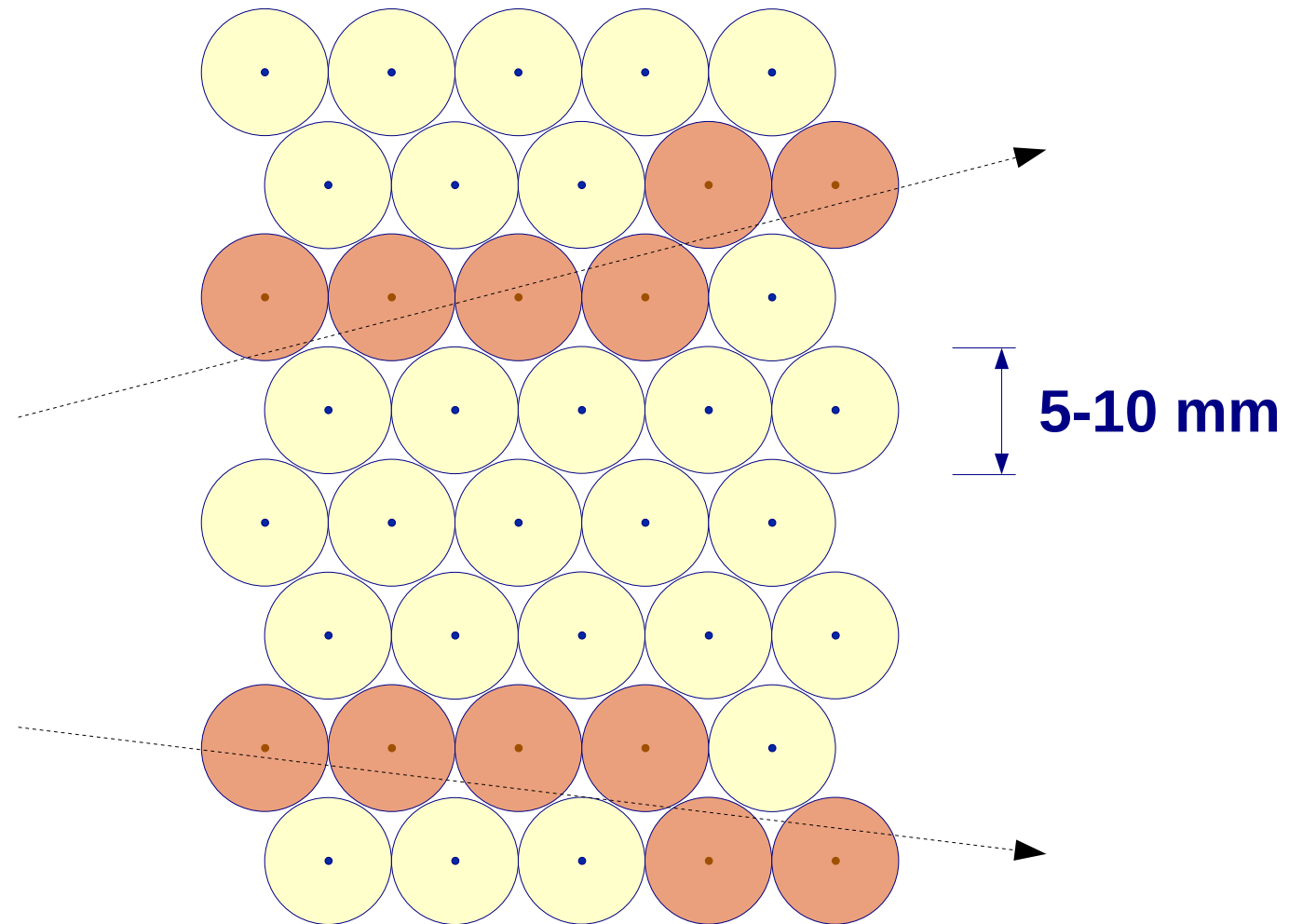
Gaseous tracking detectors

Tracking detector: several layers of such drift tubes



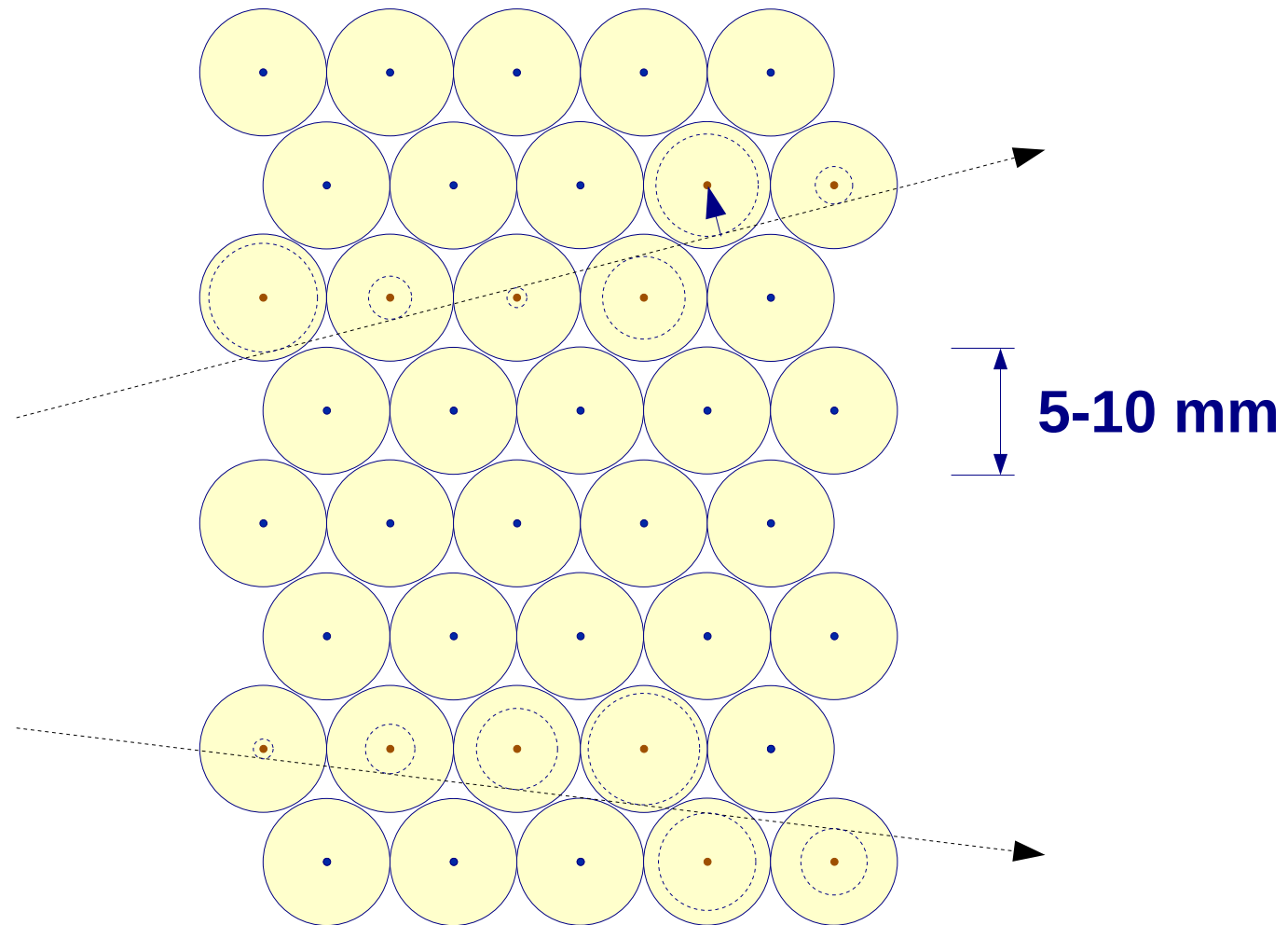
Gaseous tracking detectors

Tracking detector: several layers of such drift tubes

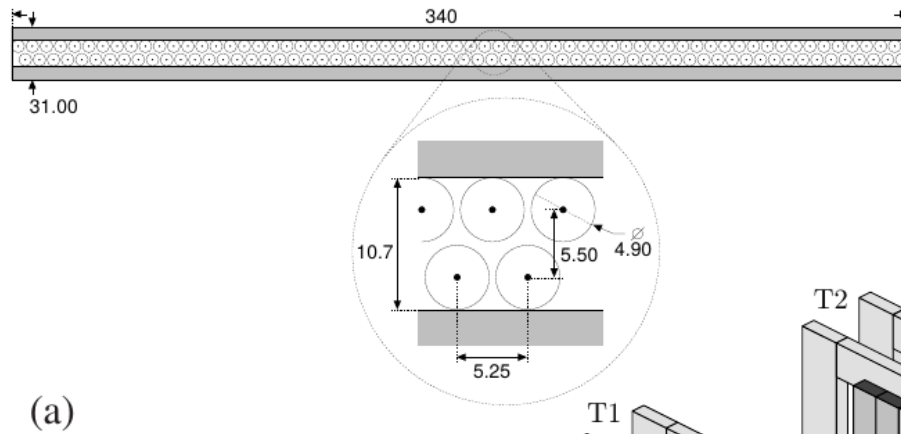


Gaseous tracking detectors

Measure drift time of electrons \rightarrow $< 200 \mu\text{m}$ spatial resolution

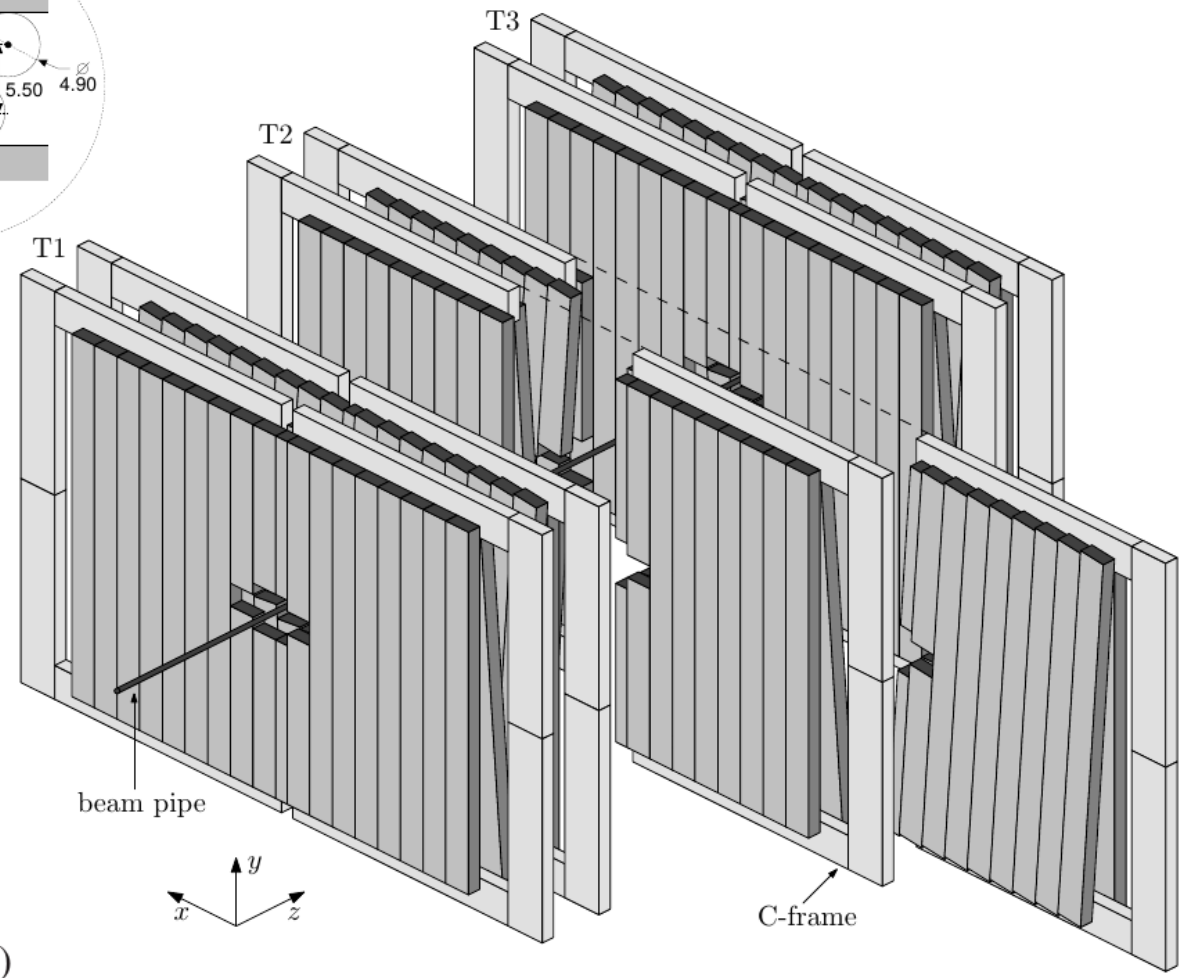


LHCb Outer Tracker



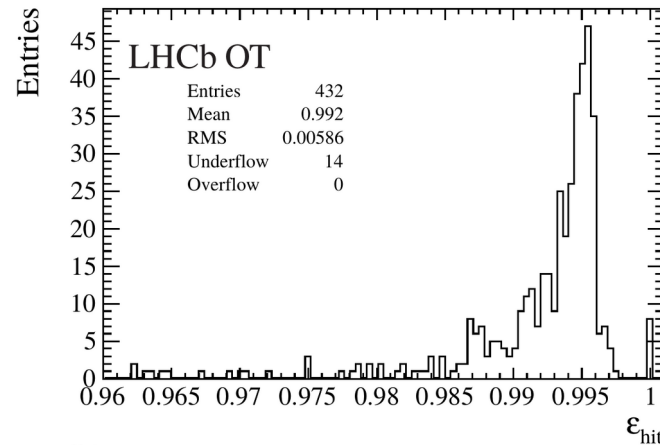
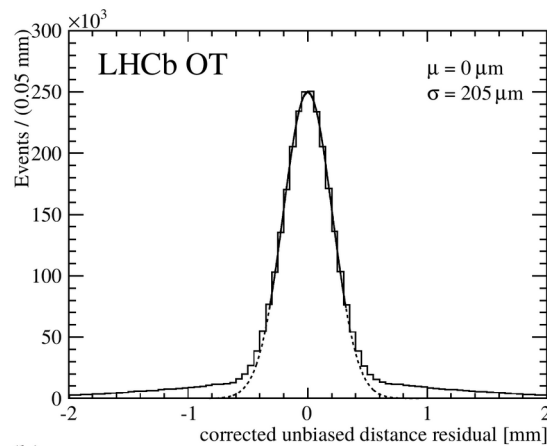
(a)

**Covers $12 \times 30 \text{ m}^2$ with
53'760 drift tubes**
 → 2.4 m long
 → 4.9 mm diameter
 → **Ar/CO₂/O₂ (70/28.5/1.5)**
 → **1550 V**



(b)

Gaseous tracking detectors

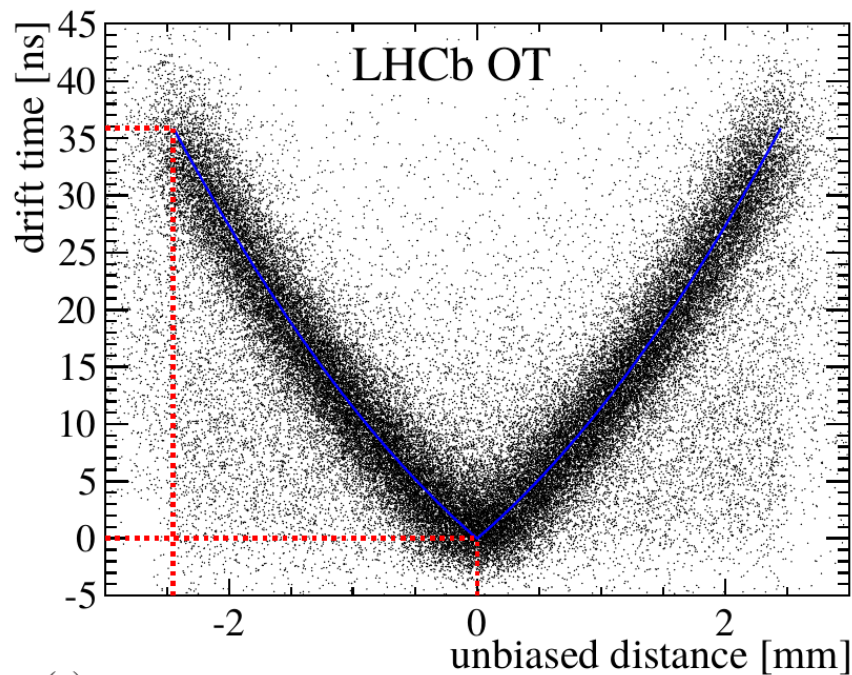


- operated reliably
- good spatial resolution $\approx 200 \mu\text{m}$
- good hit efficiency $> 99 \%$
- is being replaced by a scintillating fibre tracker in the ongoing LHCb upgrade

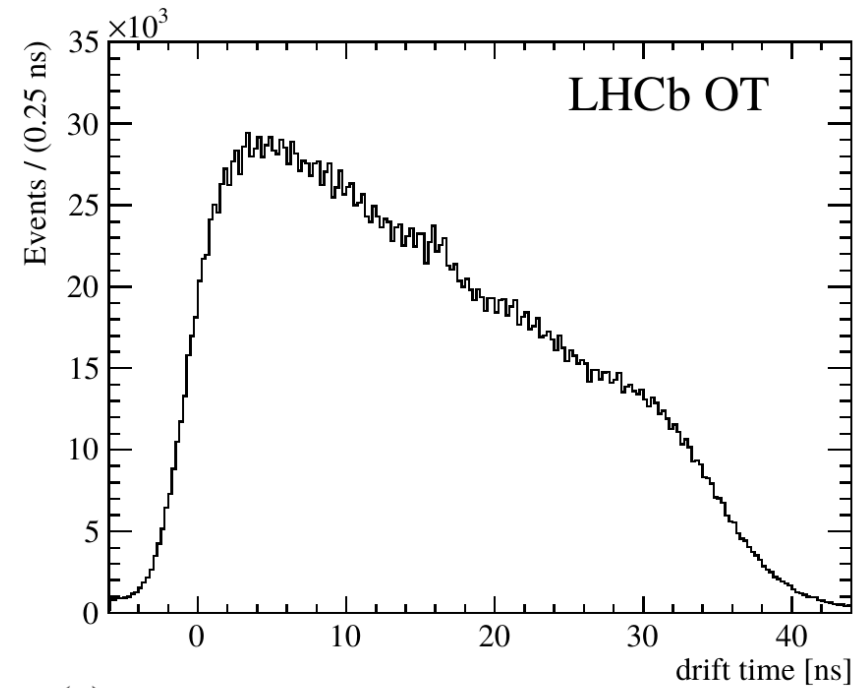
LHCb Outer Tracker

Drift time of electrons up to ≈ 40 ns,
but bunch crossings at the LHC every 25 ns

→ read out overlapping events



(a)



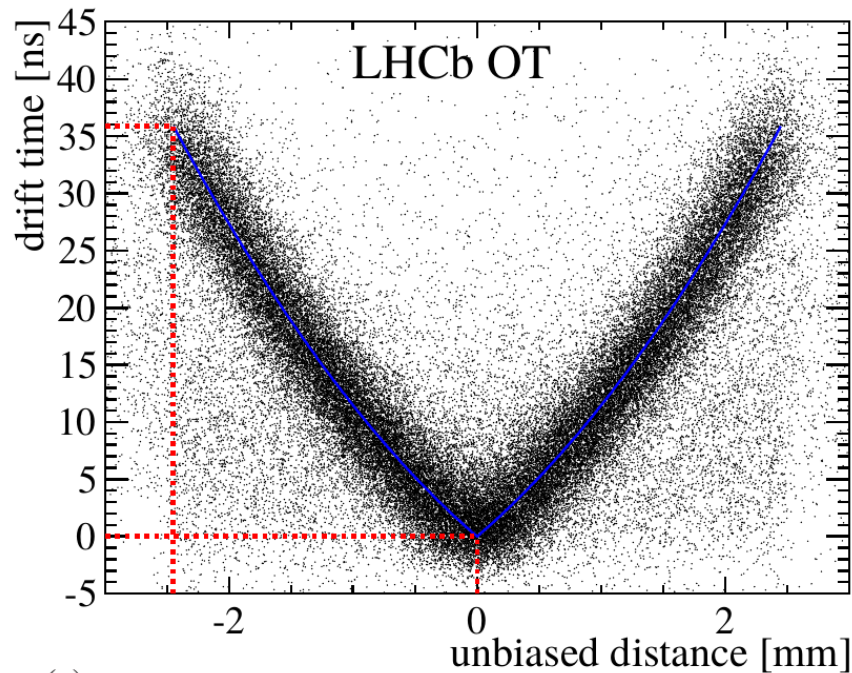
(c)

[JINST9(2014)P01002]

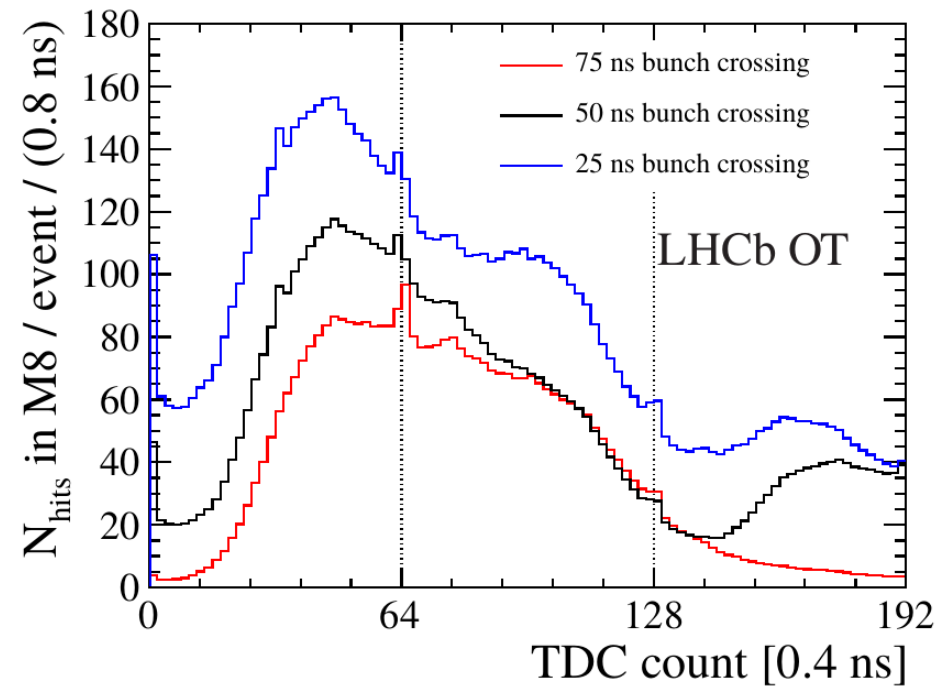
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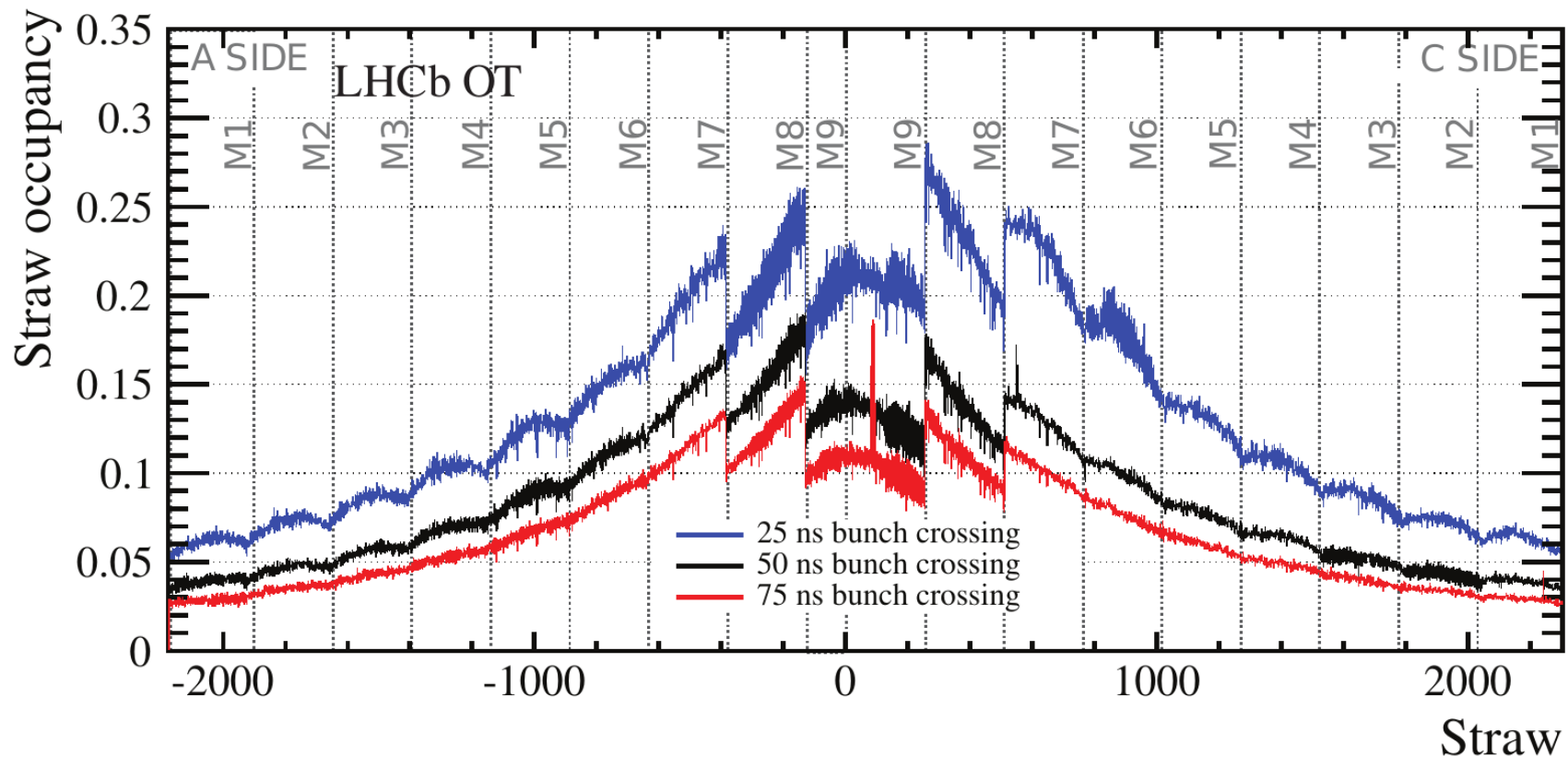
(a)



[JINST9(2014)P01002]

LHCb Outer Tracker

- Occupancy in the inner part of the detector**
- up to one in 4 straws is hit on average
 - at the limit for efficient track reconstruction



[JINST9(2014)P010002]

LHCb Outer Tracker

Primary ionization is a statistical process,
discrete ionization clusters generated
along the particle trajectory

Number of clusters for a given pathlength
follows a Poisson distribution

$$P(k | \mu) = \frac{\mu^k}{k!} \cdot e^{-\mu}$$

→ probability to create at least one cluster

$$\varepsilon = 1 - P(0 | \mu) = 1 - e^{-\mu}$$

→ for detection efficiency $\varepsilon > 99\%$ need $\mu \geq 5$

For Argon (at 1 bar): $\mu = 29$ primary clusters / cm

→ need ≥ 1.7 mm path length to reach $\varepsilon \geq 99\%$

→ need drift cell with ≥ 5 mm diameter

Gas	Density ρ [g/cm ³]	I_0 [eV]	W [eV]	n_p [cm ⁻¹]	n_T [cm ⁻¹]
H ₂	8.99×10^{-5}	15.4	37	5.2	9.2
He	1.78×10^{-4}	24.6	41	5.9	7.8
N ₂	1.23×10^{-3}	15.5	35	10	56
O ₂	1.43×10^{-3}	12.2	31	22	73
Ne	9.00×10^{-4}	21.6	36	12	39
Ar	1.78×10^{-3}	15.8	26	29	94
Kr	3.74×10^{-3}	14.0	24	22	192
Xe	5.89×10^{-3}	12.1	22	44	307
CO ₂	1.98×10^{-3}	13.7	33	34	91
CH ₄	7.17×10^{-4}	13.1	28	16	53
C ₄ H ₁₀	2.67×10^{-3}	10.8	23	46	195

Wire Ageing

Creation of chemical radicals in the charge avalanche close to the wire

→ polymerization of carbohydrates

Formation of deposits on wires

→ loss of gas gain

Formation of whiskers

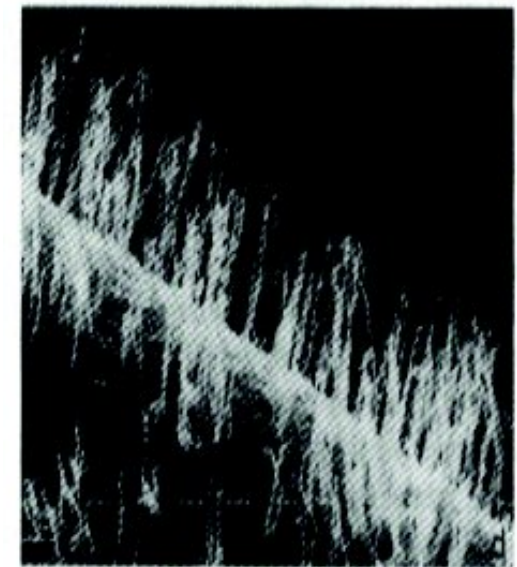
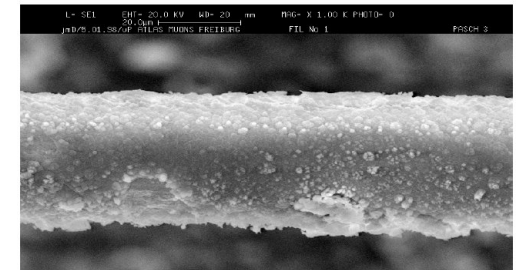
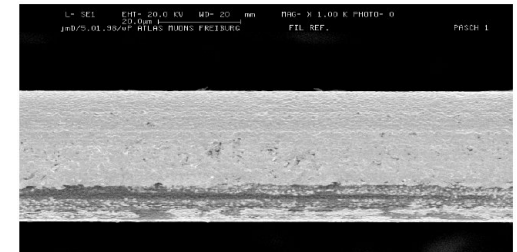
→ discharges, noise, HV breakdown

Very small contamination of the drift gas can have disastrous consequences

→ typical problem: outgassing of glues

Extensive studies, lists of “allowed” materials

→ but one mistake can destroy the detector



Micro-Pattern Gaseous Detectors

Gas Electron Multiplier (“GEM”):

Thin Kapton foil

**(electrically insulating polyimide film)
with copper coating on both sides**

Regular array of fine holes

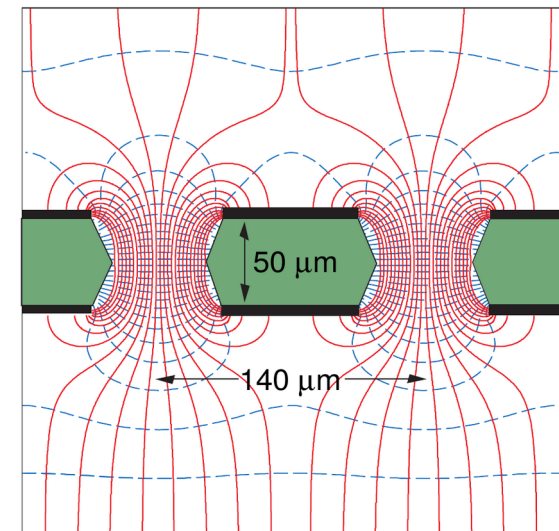
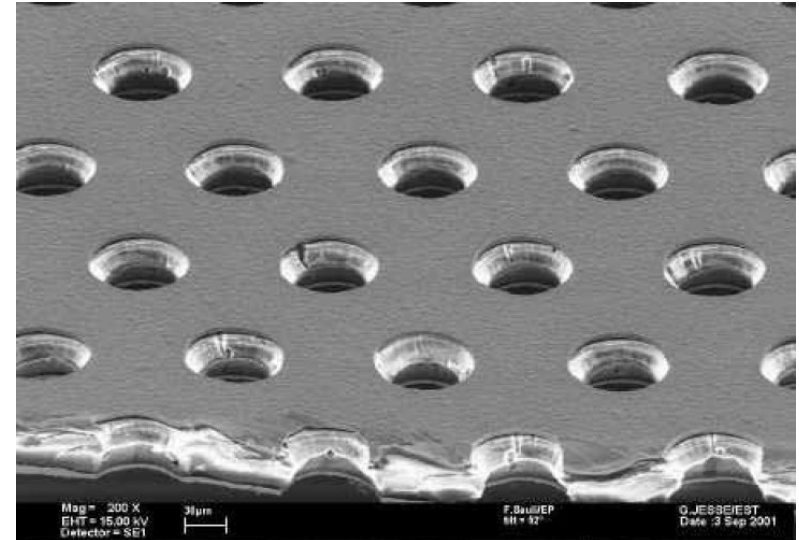
(75 μm \varnothing , 140 μm distance)

etched through the foil

Voltage applied between the two sides

→ high electric field inside the holes

→ gas amplification



Micro-Pattern Gaseous Detectors

Readout granularity independent of the thickness of the gas layer

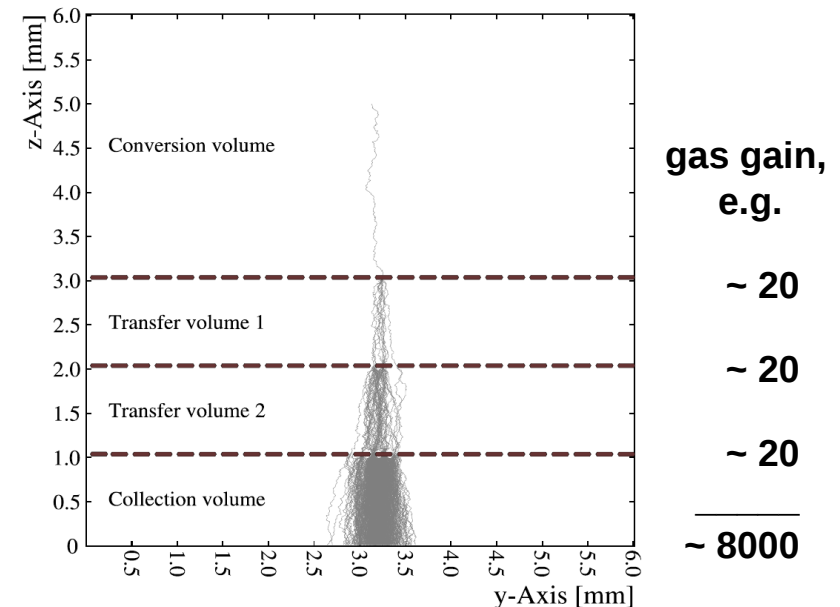
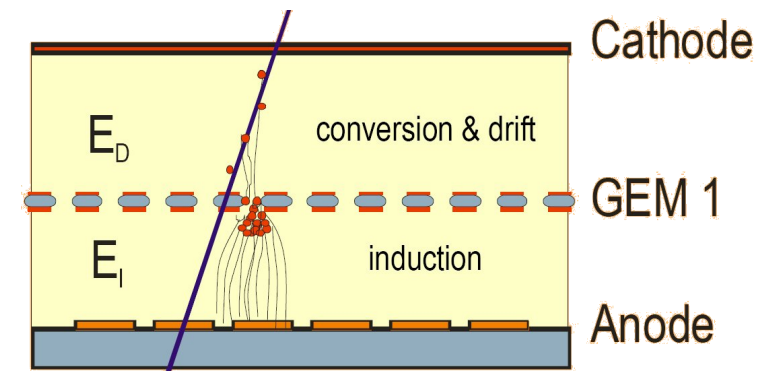
No wires → no wire ageing

Usually stack several GEM foils to obtain high gas gain with low voltage

Triple-GEM detectors e.g. employed in inner part of LHCb muon system

415 V per GEM foil → total gain ~ 4'300

Disadvantage: inclined tracks can give signals on many readout strips



Silicon tracking detectors

Segmented reverse biased $p-n$ junction (diode)

Simplest device: n -doped monocrystalline silicon wafer, p -doped implants at surface

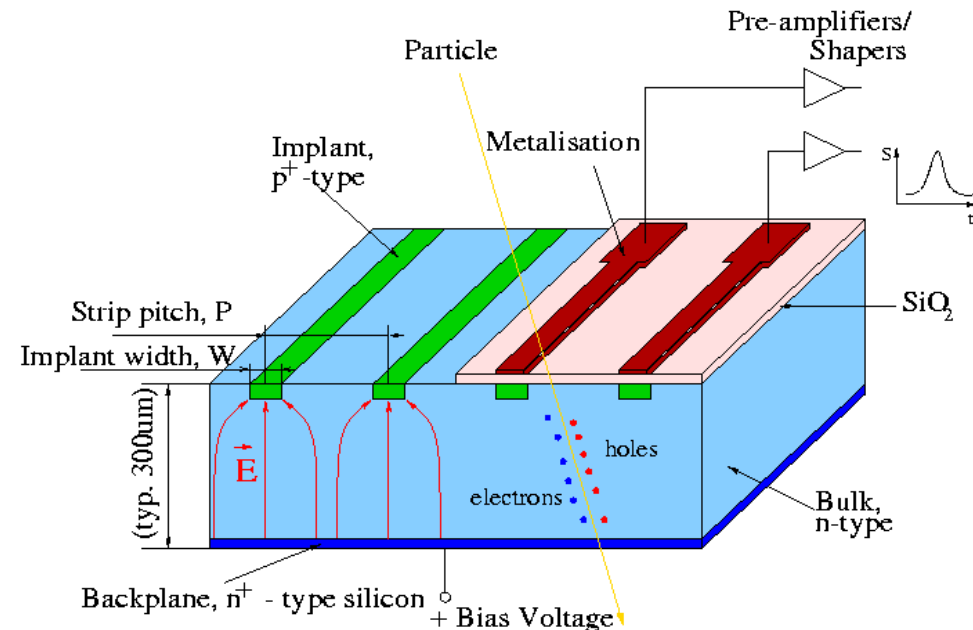
- strips with pitch 250 – 20 μm
- resolution 50 to a few μm
- or pixels for even finer granularity

Apply reverse bias voltage

- electric field through the wafer

Ionizing particle creates electron-hole pairs in the silicon lattice

- electrons and holes drift to surface
- induce signals on the p -doped implants



p-n Junction

n-side: doping with Group-V elements

→ loosely bound electrons (e) in silicon lattice

p-side: doping with Group-III elements

→ loosely bound “holes” (h) in silicon lattice

e/h density gradient across the junction

→ diffusion across the junction

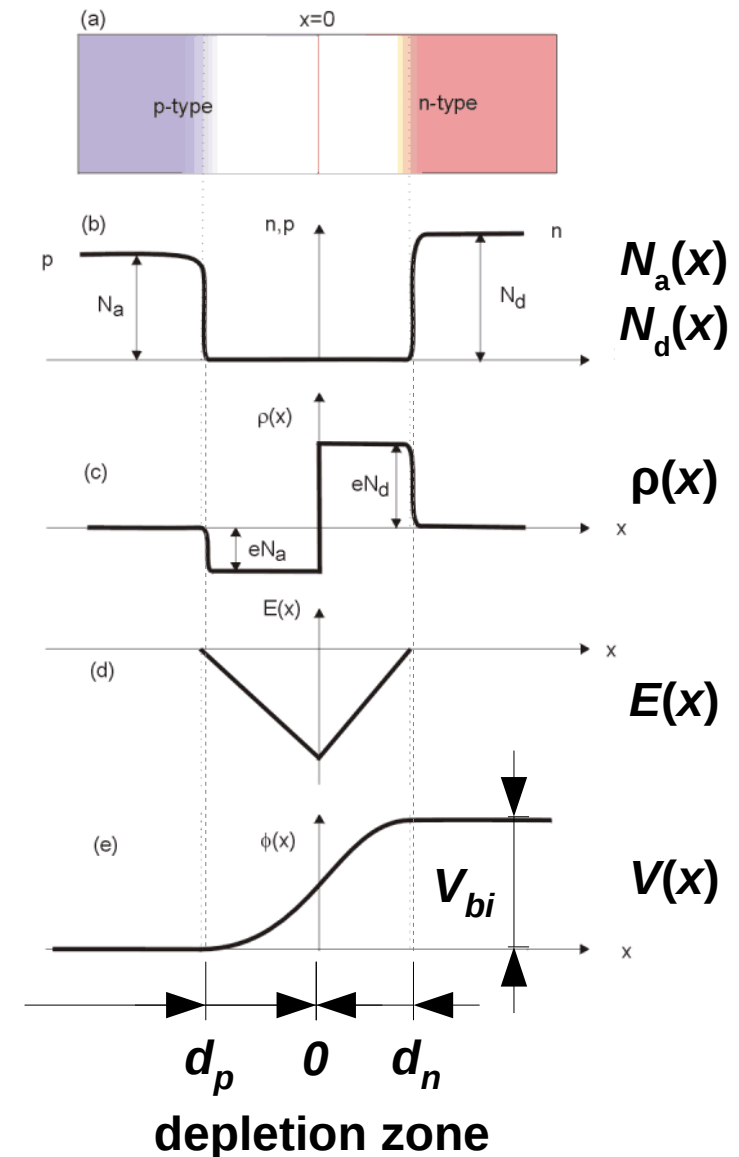
Depletion zone without free charge-carriers

→ p-side: e absorbed by acceptor atoms

→ n-side: h absorbed by donor atoms

Movement of electric charge

→ electric field across the junction



p-n Junction

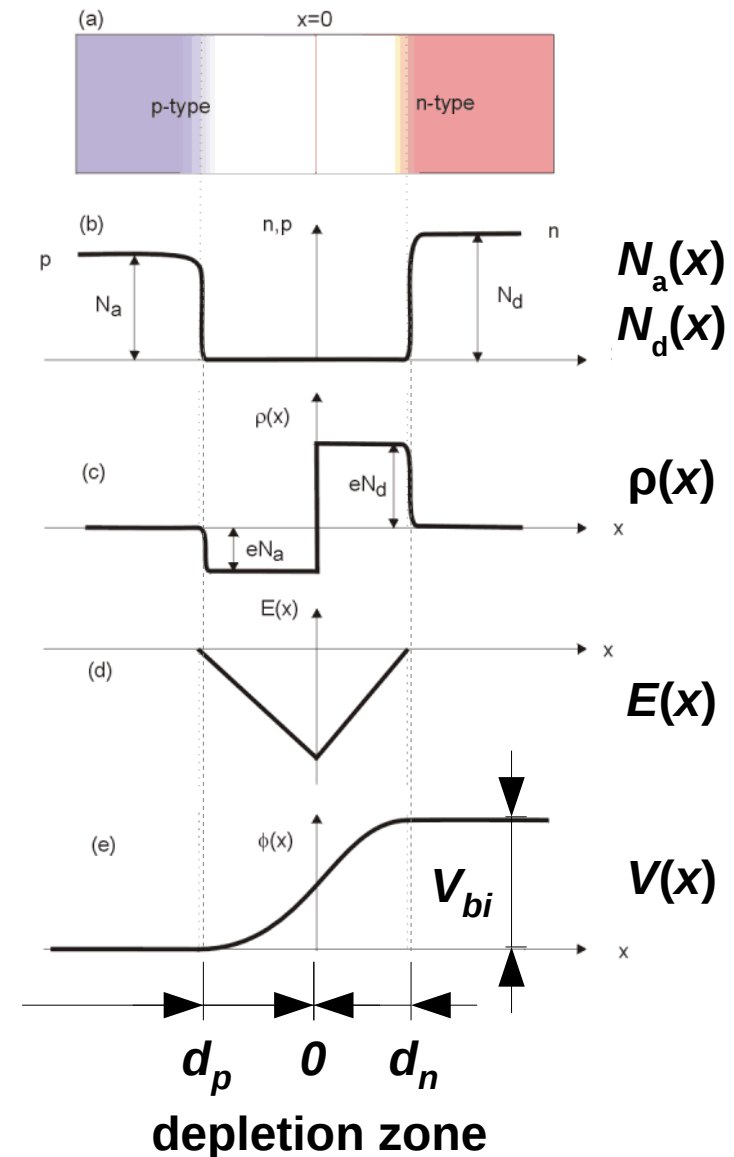
Equilibrium between diffusion and Coulomb force

Electric field and potential barrier from Coulomb equation

$$-\frac{d^2 V}{dx^2} = \frac{dE}{dx} = \frac{\rho(x)}{\epsilon}$$

→ intrinsic potential barrier and thickness of depletion zone:

$$V_{bi} = \frac{e}{2\epsilon} \cdot (N_d d_n^2 + N_a d_p^2)$$



Asymmetric Junction

In a silicon detector, junction is between

- bulk: few 100 μm thick
- implants: few μm thin

Want depletion zone to extend into bulk

$$d_n (\text{bulk}) \gg d_p (\text{implant})$$

To achieve this, use charge conservation

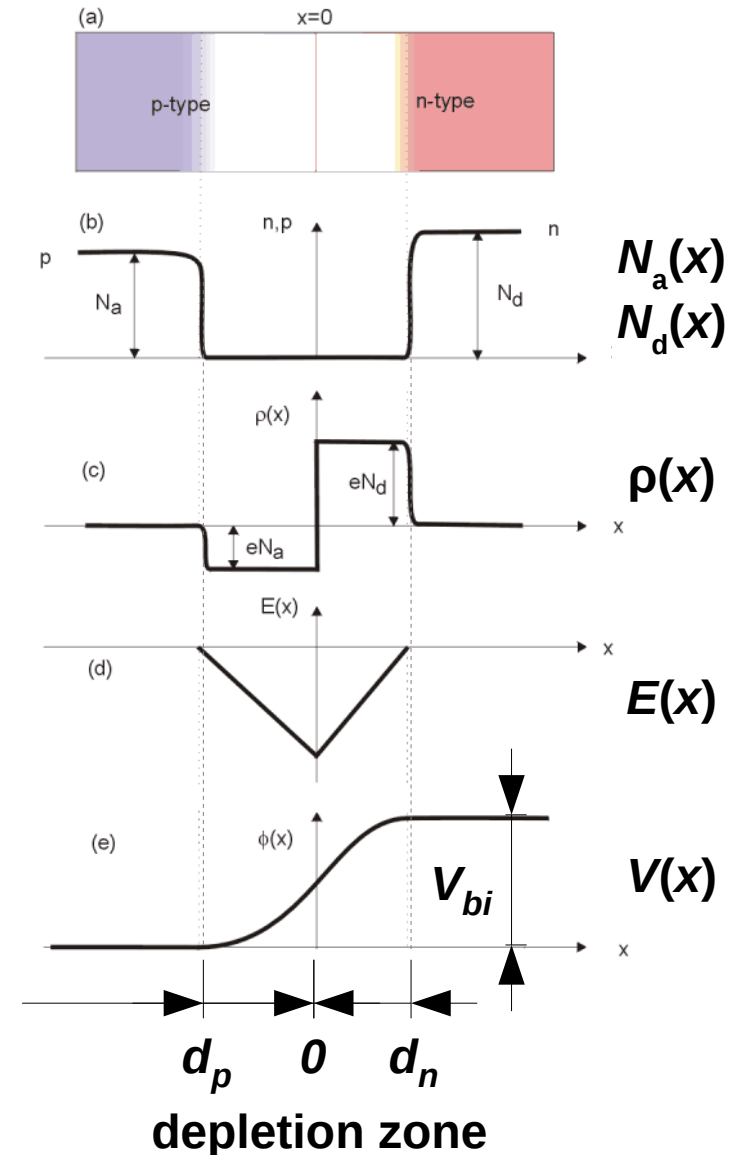
$$N_d d_n = N_a d_p$$

and make

$$N_a (\text{implant}) \gg N_d (\text{bulk})$$

For $d_n \gg d_p$:

$$V_{bi} = \frac{e}{2\epsilon} \cdot N_d d_n^2 \Leftrightarrow d_n = \sqrt{\frac{2\epsilon V_{bi}}{e} \cdot \frac{1}{N_d}}$$



Reverse-Biased Junction

Example: $N_d \approx \text{few} \times 10^{12} / \text{cm}^3$

$\rightarrow V_{bi} = 0.65 \text{ V}, d_n \approx 25 \mu\text{m}$

Apply an external voltage to increase the thickness of depletion zone

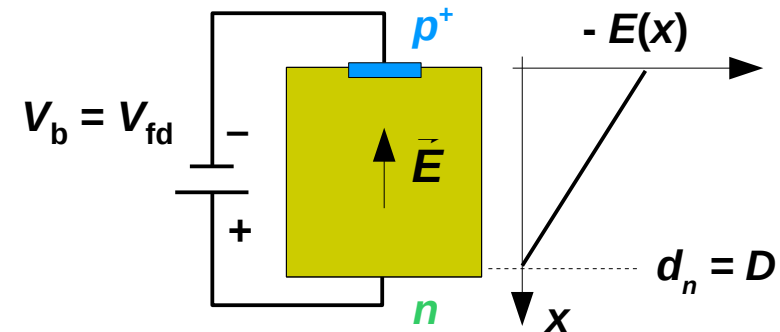
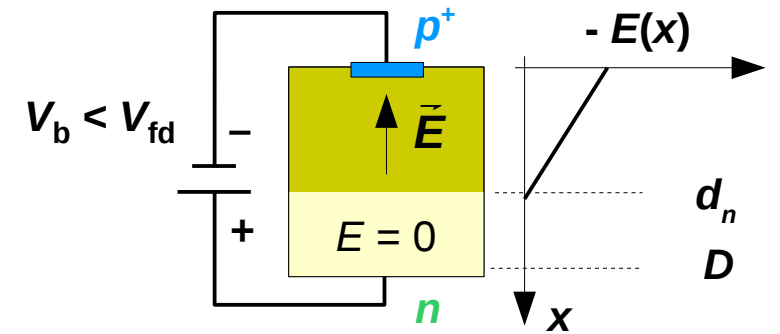
$$d_n = \sqrt{\frac{2\varepsilon (V_b + V_{bi})}{e} \cdot \frac{1}{N_d}}$$

To fully deplete a detector of thickness D

$$V_{fd} = \frac{e}{2\varepsilon} \cdot N_d \cdot D^2$$

Example: $D = 300 \mu\text{m}, N_d \approx \text{few} \times 10^{12} / \text{cm}^3$

$$V_{fd} \approx 100 \text{ V}$$



Charge Collection

Drift velocity of charge carriers proportional to electric field $E(x)$

$$\mathbf{v}(x) = \mu \cdot \mathbf{E}(x)$$

with $\mu \equiv$ charge carrier “mobility”

$\approx 1500 \text{ cm}^2 / \text{Vs}$ for electrons

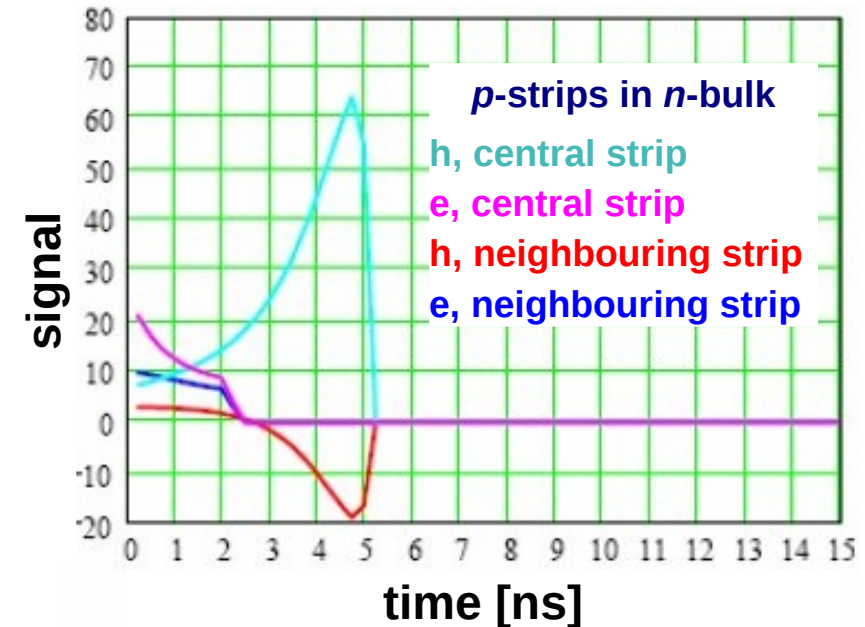
$\approx 450 \text{ cm}^2 / \text{Vs}$ for holes

Maximum drift time (for $V_b \gg V_{fd}$)

$$t_{\max} = \frac{D^2}{2 \mu \cdot V_b}$$

Example: $D = 300 \text{ } \mu\text{m}$, $V_b = 200 \text{ V}$

$$t_{\max} \approx \begin{cases} 3.5 \text{ ns} & \text{for electrons} \\ 11 \text{ ns} & \text{for holes} \end{cases}$$



Signal on readout strips induced by moving charge carriers

- h drift towards the implant,
- e drift towards backplane

Signal and Noise

“Signal” from charged particle

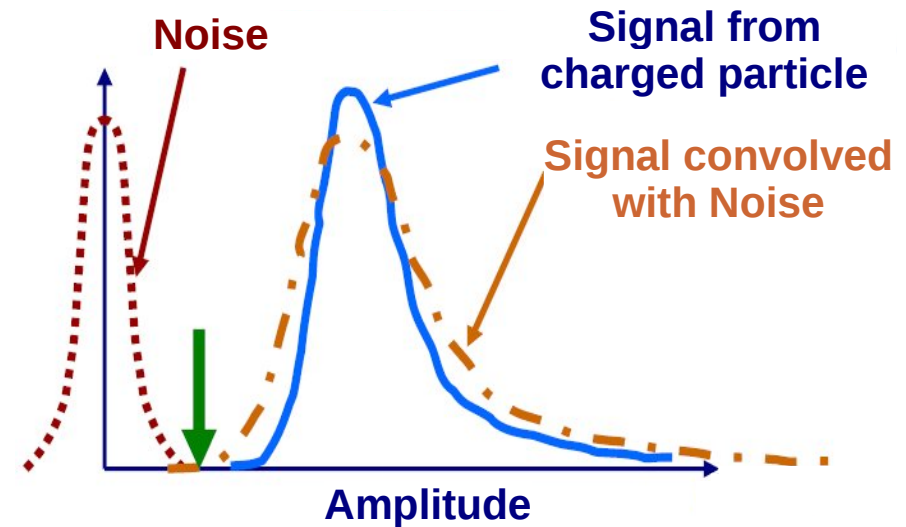
→ Landau distribution

“Noise”, e.g. from electronics

→ Gaussian with mean zero

→ broadens also signal distribution

**Cut on the measured amplitude
to select signal and suppress noise**



For high detection efficiency at low rate of “noise hits”
need clean separation between the distributions

Figure of merit: $S/N \equiv \frac{\text{most probable signal for mip}}{\text{rms of noise distribution}}$

Rule of thumb: need $S/N > 10$ for a working detector

Signal and Noise

**Signal determined by dE/dx of particle
and thickness of depletion zone**

→ e.g. most probably signal of 22'500 e/h pairs
for a minimum-ionizing particle in a 300 μm thick detector

Various noise sources:

Fluctuations in leakage currents

→ operate at low temperature

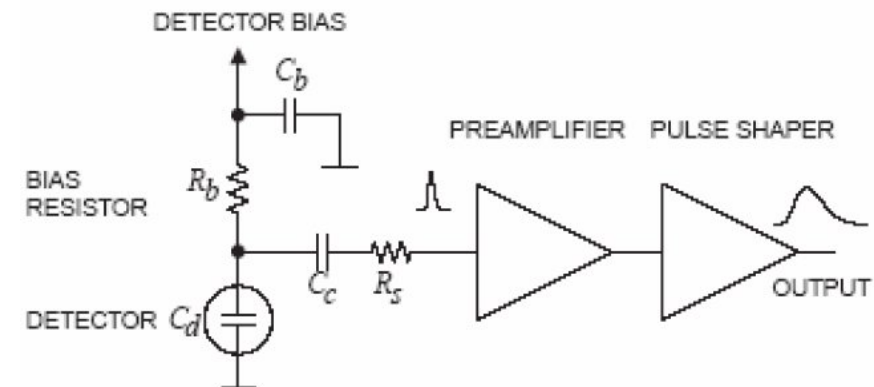
Voltage fluctuations in resistors

→ R_s as small as possible

→ R_b as large as possible

Detector capacitance

→ strip / pixel size



C_d : sensor capacitance to ground

R_b : bias resistor

C_c : AC coupling capacitance

R_s : serial resistance on signal path

Silicon Strip Detector

Basic features of a *p-in-n* strip sensor

metallization of readout strips and backplane

reduce electric resistance (R_s) along signal path

thin SiO layer between implants and metal strips

isolate readout amplifier from leakage currents through detector bulk (“AC coupled readout”)

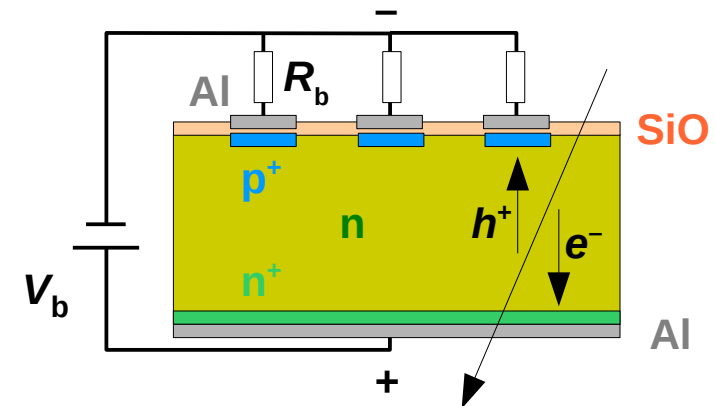
bond pads: connect metal strip to readout electronics

DC pads: ohmic contact to p^+ implant, for test purposes

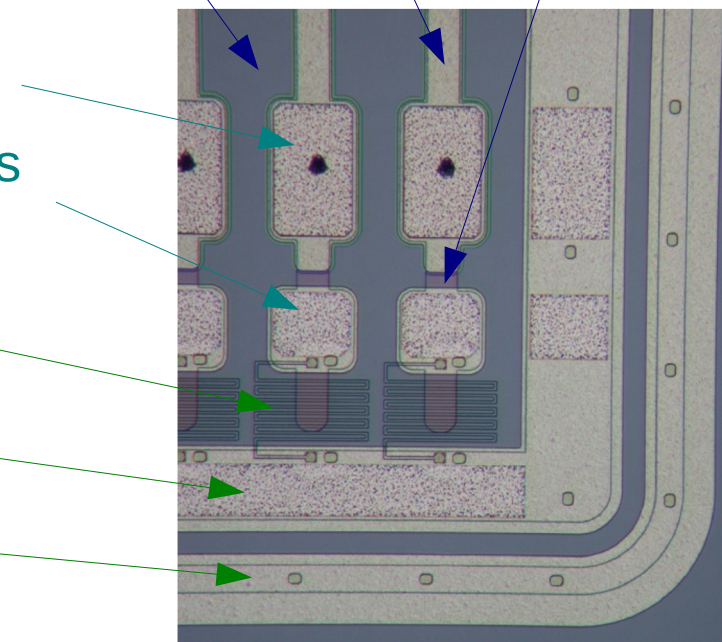
bias resistors: connect p^+ implants to bias ring, but insulate implants from each other

bias ring: connect to external bias voltage

guard ring(s): shape electric field close to the edge of the sensor, avoid discharges to backplane



n bulk Al strip p^+ implant



Pixel Detectors

Readout implants segmented into pixels (typically $\approx 50 \times 500 \mu\text{m}^2$)

Finer segmentation

→ higher rate capability

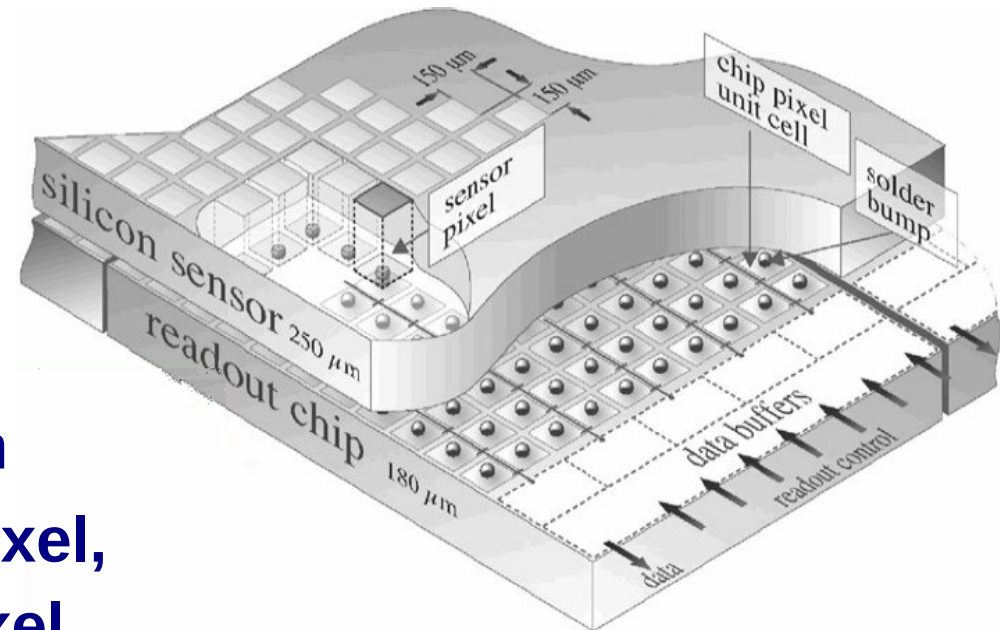
Smaller cell size

→ lower noise

Measure both coordinates

→ easier for track reconstruction

**Need readout amplifier for each pixel,
located directly on top of the pixel**



Hybrid detector: two wafers mounted back-to-back

1st wafer: pixel sensor, 2nd wafer: readout electronics

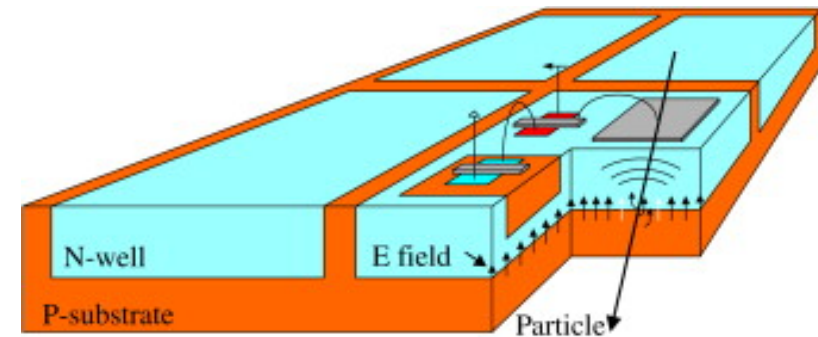
electrical connection by “bump bonding”

Monolithic Pixels

Integrate detector and front-end electronics in one wafer

Smaller capacitance → lower noise

- do not need large signal
- can make detectors very thin
- do not need large bias voltage



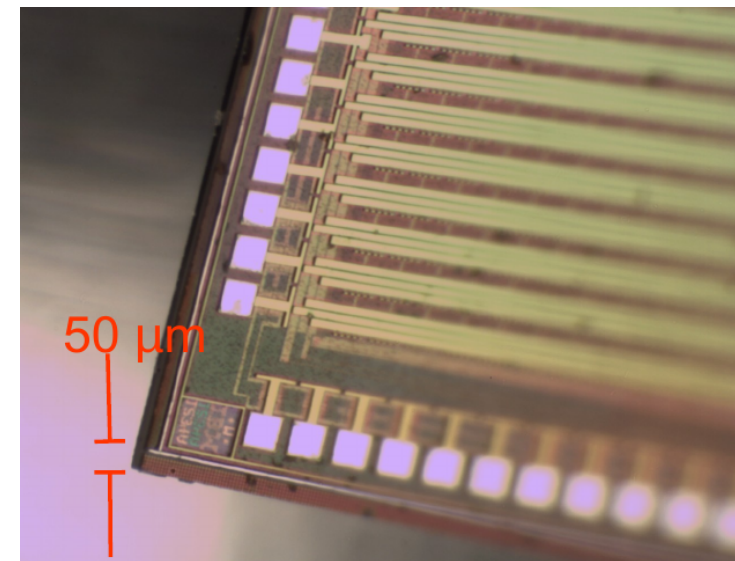
Example: High-Voltage CMOS

- process developed for automobile industry
- allows to apply voltages up to 100 V

Developed for $\mu 3e$ experiment at PSI:

- thickness $50 \mu\text{m}$, pixels $\approx 80 \times 80 \mu\text{m}^2$

Envisaged for LHCb upgrade 1b and 2



Low-Gain Avalanche Detectors

Thin, highly doped “gain layer”
underneath each readout implant

- high electric field
- charge avalanche

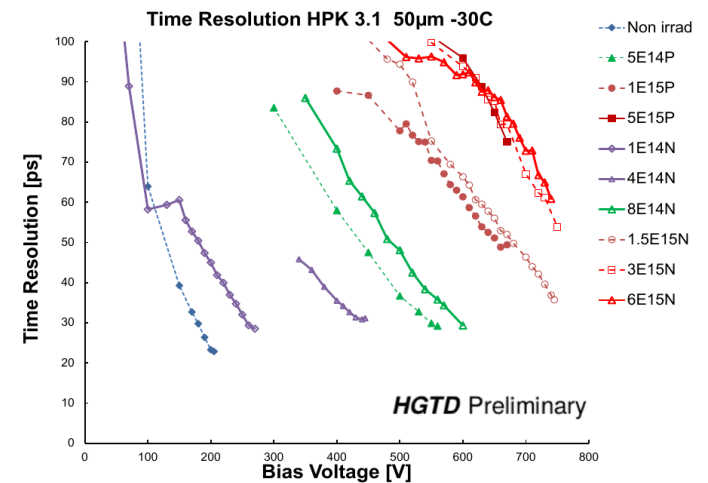
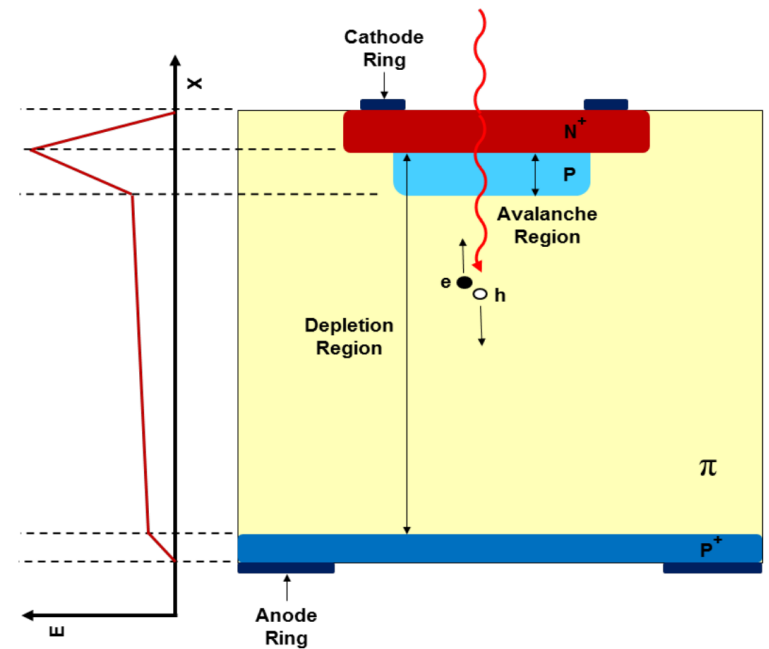
Large signal despite thin sensor

- fast signal collection
- time resolution of 30 ps
for large pixels ($1.3 \times 1.3 \text{ mm}^2$)

Time resolution for small pixels ?

- non-uniform electric field
- non-uniform drift velocity

Radiation hardness ?



[Giovanni Pellegrini @ 23rd RD50]

“4D” Tracking

Measure position and time of hit

Can help with pattern recognition:

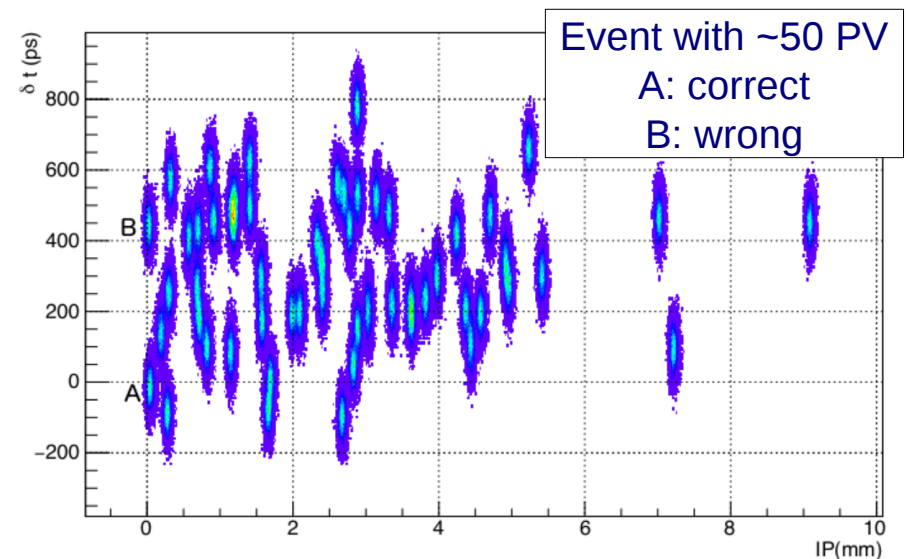
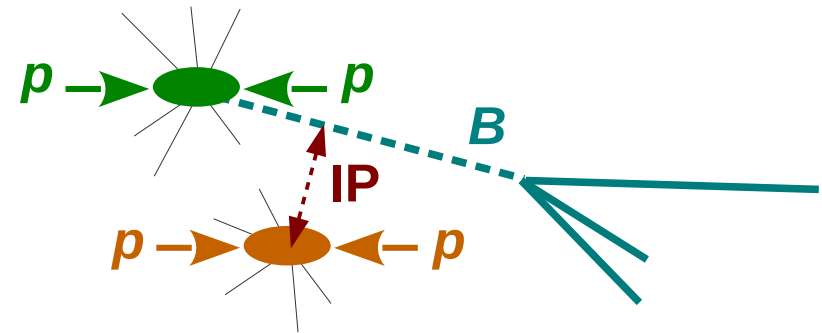
- assigning hits to tracks
- assigning tracks to vertices

E.g. LHCb measures B mesons

→ travel ~ 1 cm before they decay

**LHCb Upgrade 2: around
50 pp interaction vertices for
each LHC bunch crossing**

→ lower risk of assigning B meson
to a wrong pp vertex if precise
timing information is available



[LHCb-PUB-2019-001]

“4D” Tracking

Measure position and time of hit

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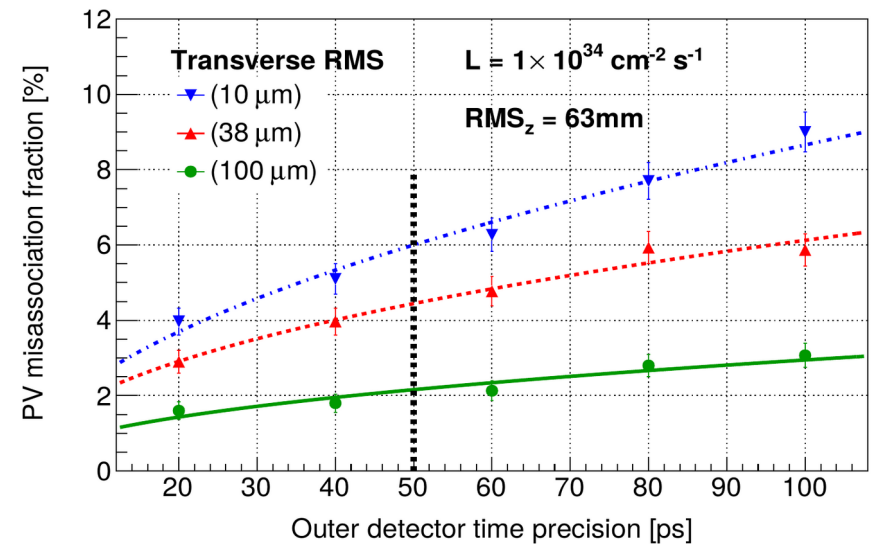
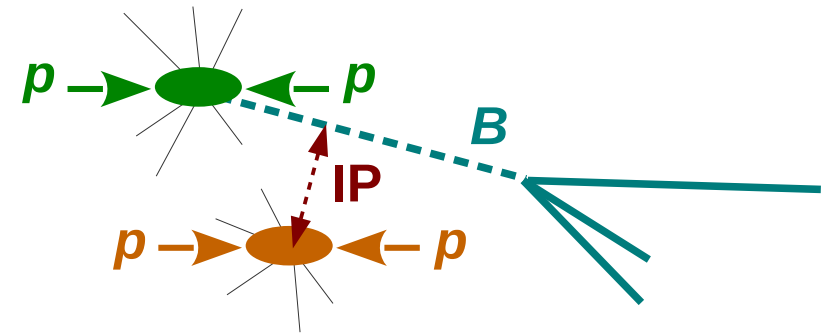
- assigning hits to tracks
- assigning tracks to vertices

E.g. LHCb measures *B* mesons

→ travel ~ 1 cm before they decay

LHCb Upgrade 2: around 50 *pp* interaction vertices for each LHC bunch crossing

→ lower risk of assigning *B* meson to a wrong *pp* vertex if precise timing information is available



[LHCb - PUB - 2019 - 001]

Radiation Damage

Most critical: bulk damage from Non-Ionising Energy Loss (NIEL)

Displacement of atoms in the lattice

→ increase of leakage current, noise

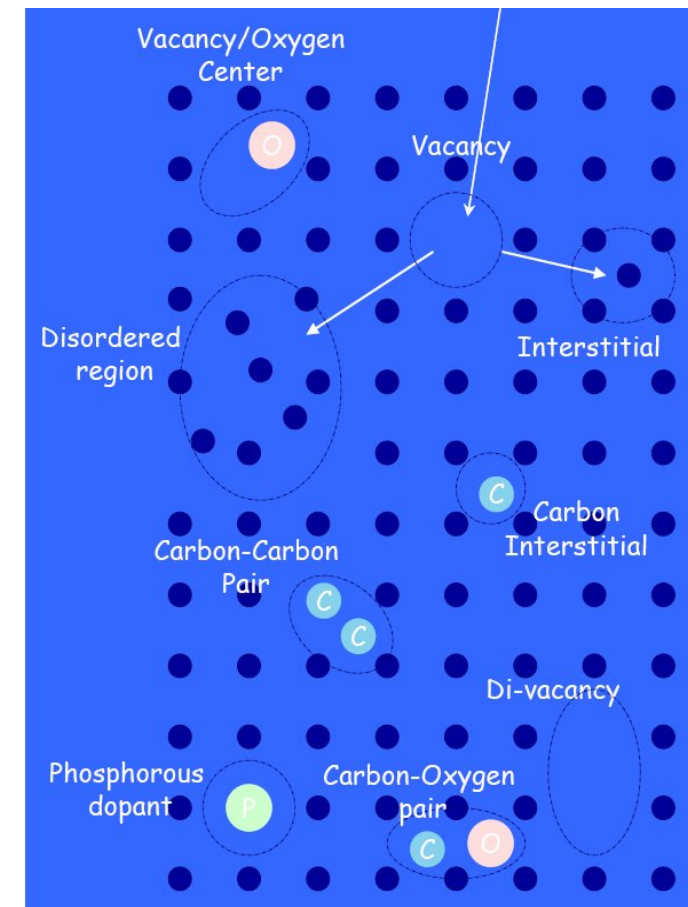
Defects act like acceptor atoms

→ “effective dopant concentration”
of the silicon bulk changes

$$N_d \rightarrow N_{\text{eff}} = N_d - N_a$$

→ “Type inversion”: bulk becomes
effectively *p*-type as number of defects
keeps increasing with received fluence

Defects can trap drifting charge carriers



Radiation Damage

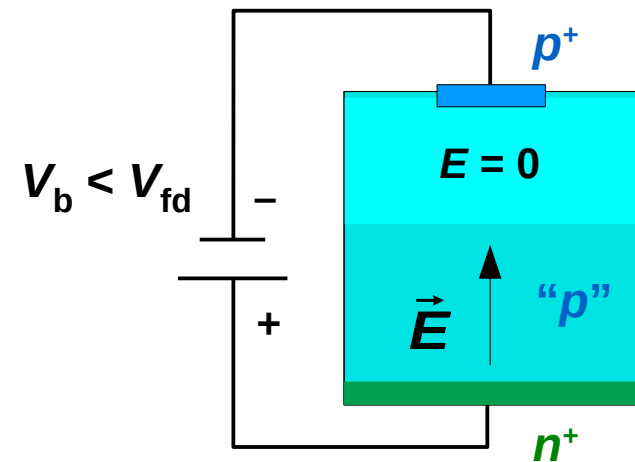
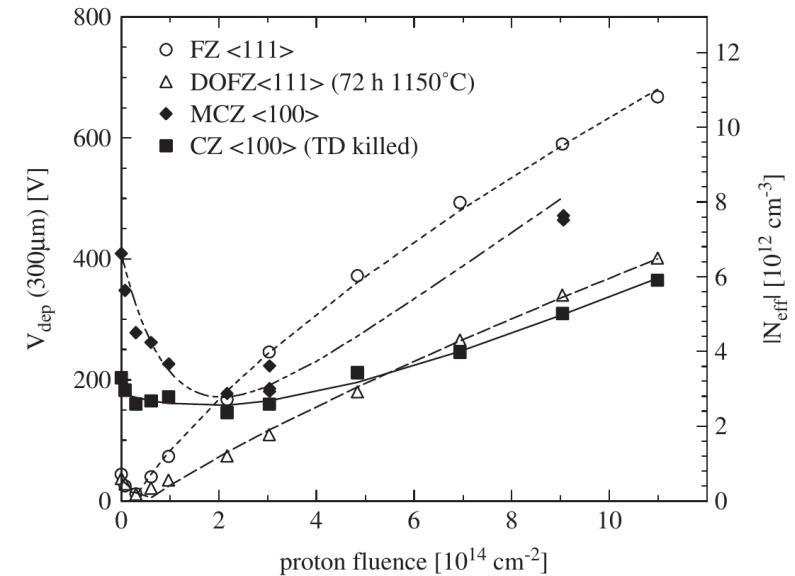
Full depletion voltage changes with effective dopant concentration

$$V_{fd} = \frac{e}{2\epsilon} \cdot |N_{eff}| \cdot D^2$$

- keeps increasing after type inversion
- eventually exceeds breakdown voltage
- cannot fully deplete the detector

After type inversion, depletion zone grows from backplane of the sensor

- field-free region on the strip side if the detector is not fully depleted
- rapid loss of efficiency, spatial resolution



Radiation Damage

Operate detectors at low temperatures

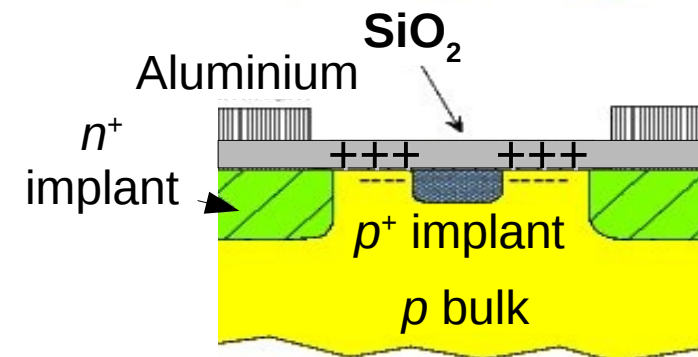
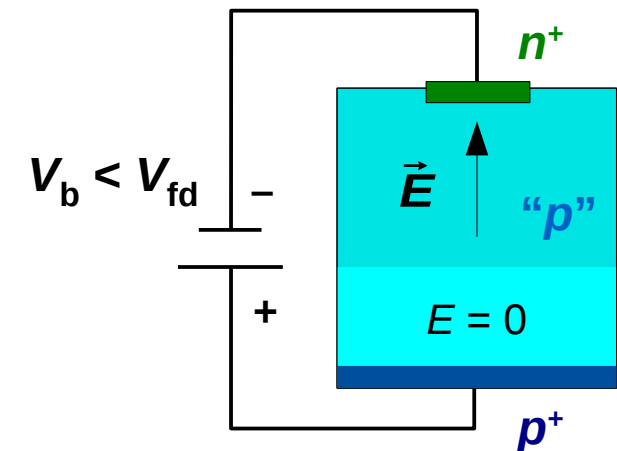
- suppresses leakage currents
- slows down change in N_{eff}

Use n -type implants in p -type bulk:

- depletion zone grows from readout side before and after irradiation
- slow, gradual loss of efficiency as V_{fd} exceeds maximal bias voltage

But: trapping of e^- at Si/SiO₂ interface:

- causes short between readout strips
- need to add p^+ -type implants to insulate n -type implants from each other
- additional production step, higher cost



“3D Detectors”

Manufacture implants through the bulk

- decouple drift distance from detector thickness

Higher rate capability

- faster charge collection

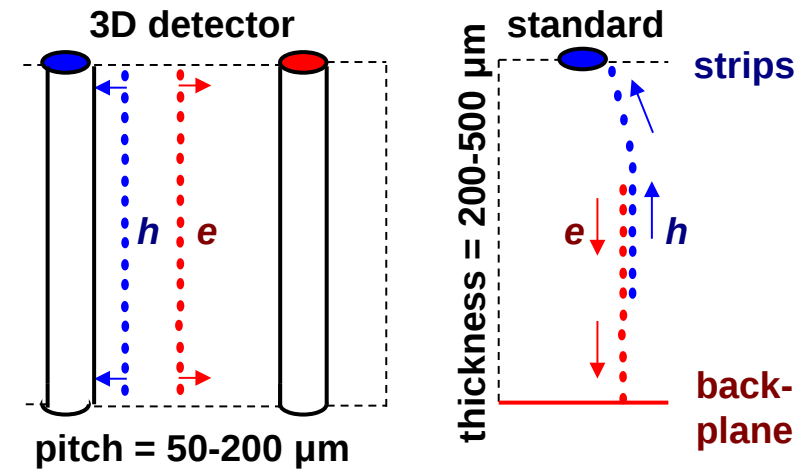
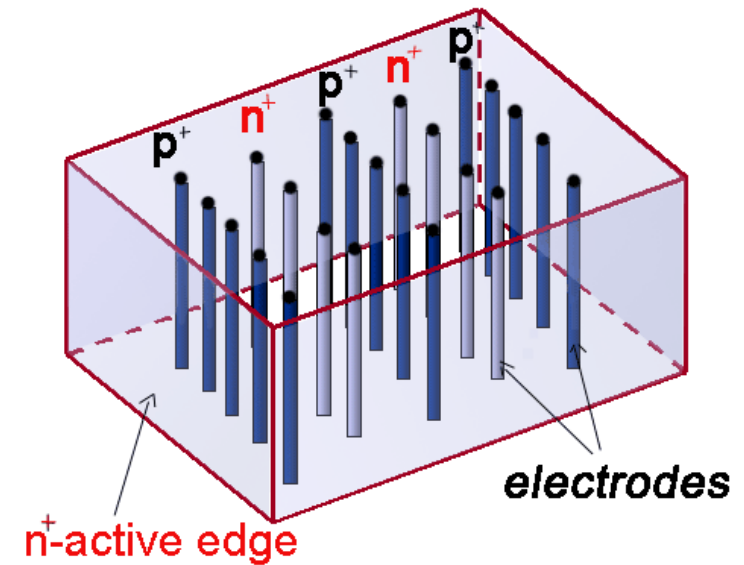
Better radiation hardness:

- lower bias voltages
- smaller losses from charge trapping

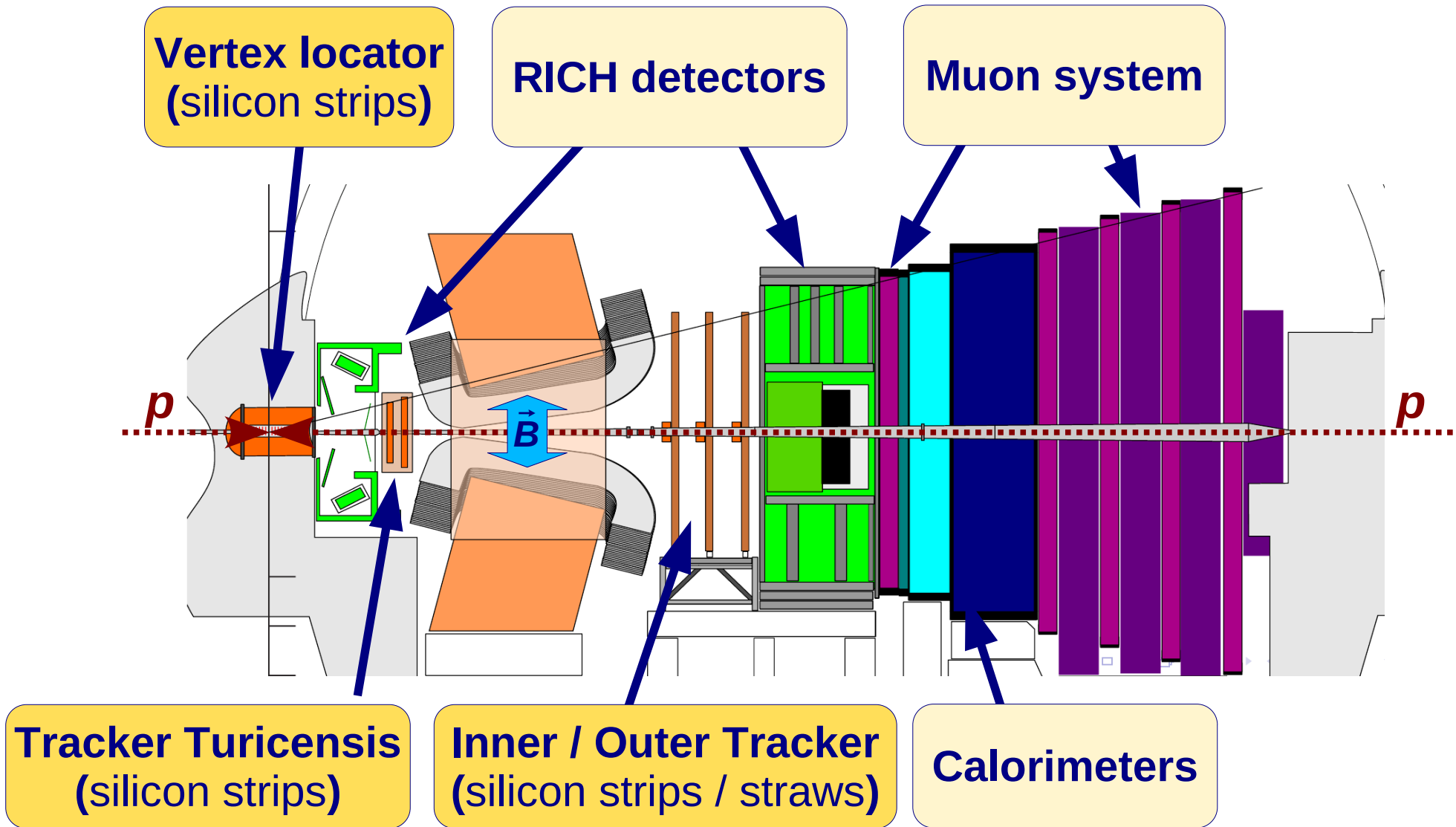
Production expensive

- laser drilling or etching

First employed in ATLAS Inner Barrel Layer, installed in 2013/2014



LHCb Detector: 2010-2018



[JINST 3(2008)S08005]

Tracking System: 2010-2018

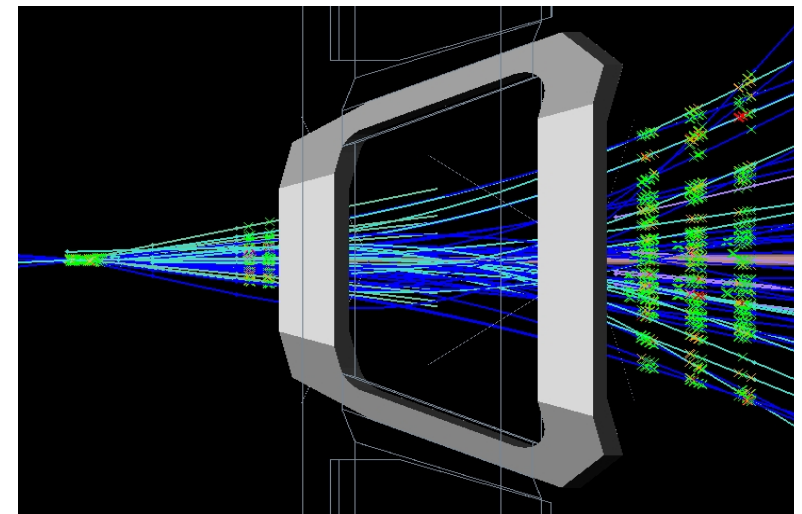
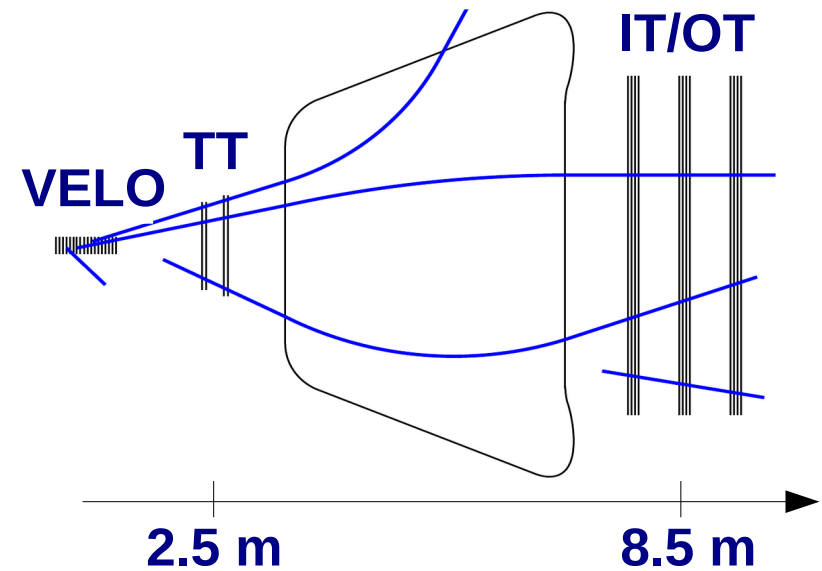
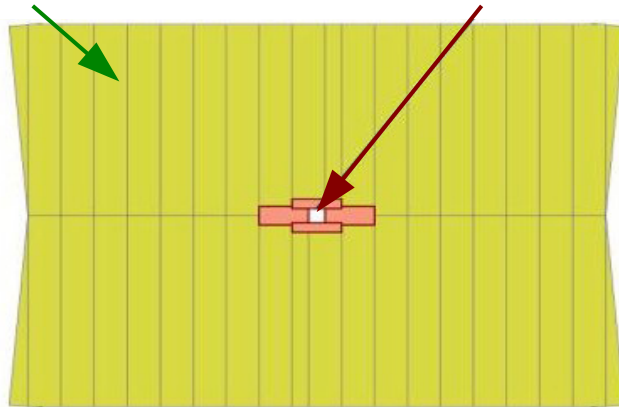
Particle density falls off rapidly with distance from the beam axis

→ finer granularity in inner region of each detector station, less fine granularity in outer regions

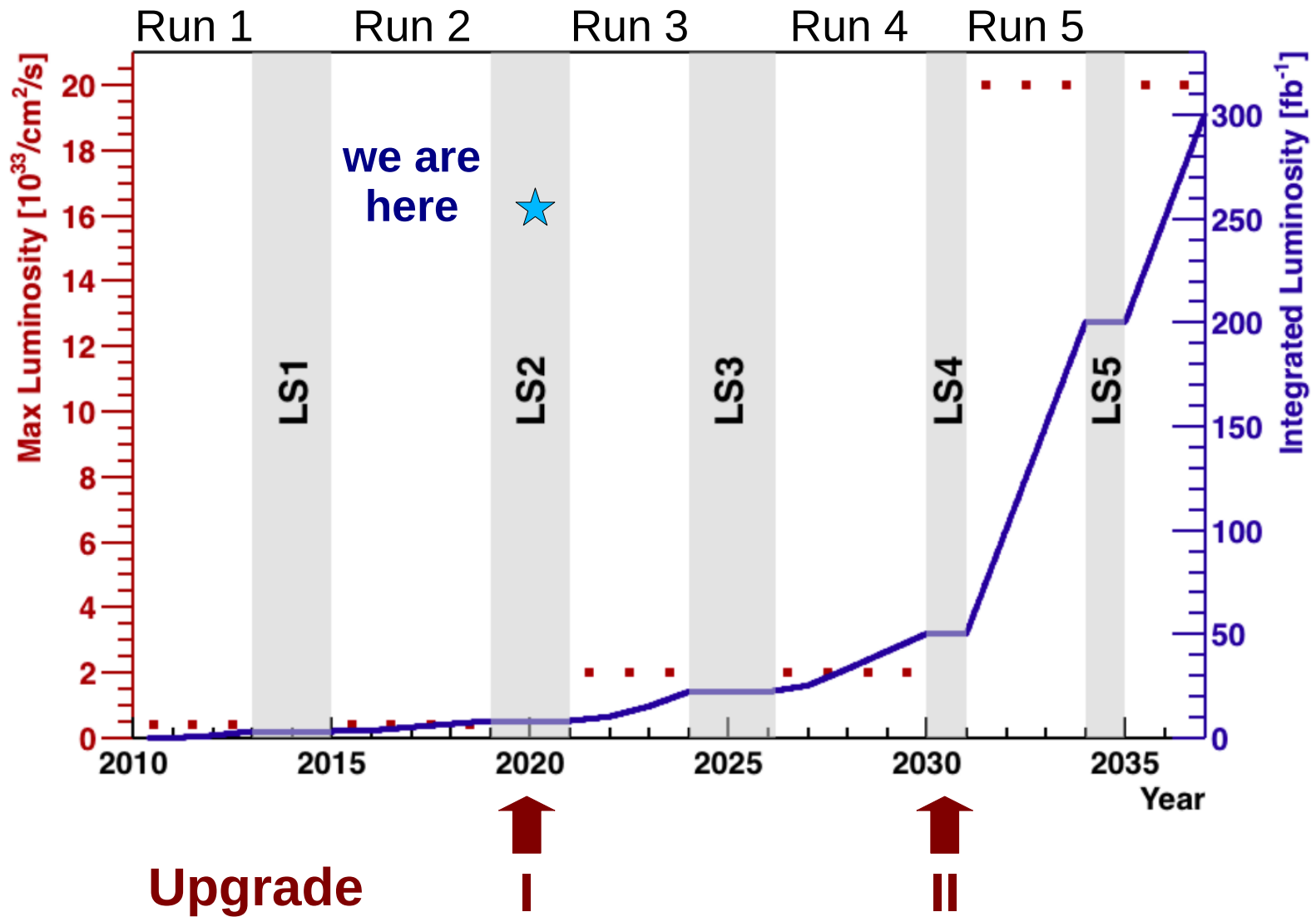
Downstream of magnet, two technologies in each station:

OT: Straws

IT: Silicon strips



LHCb Upgrades



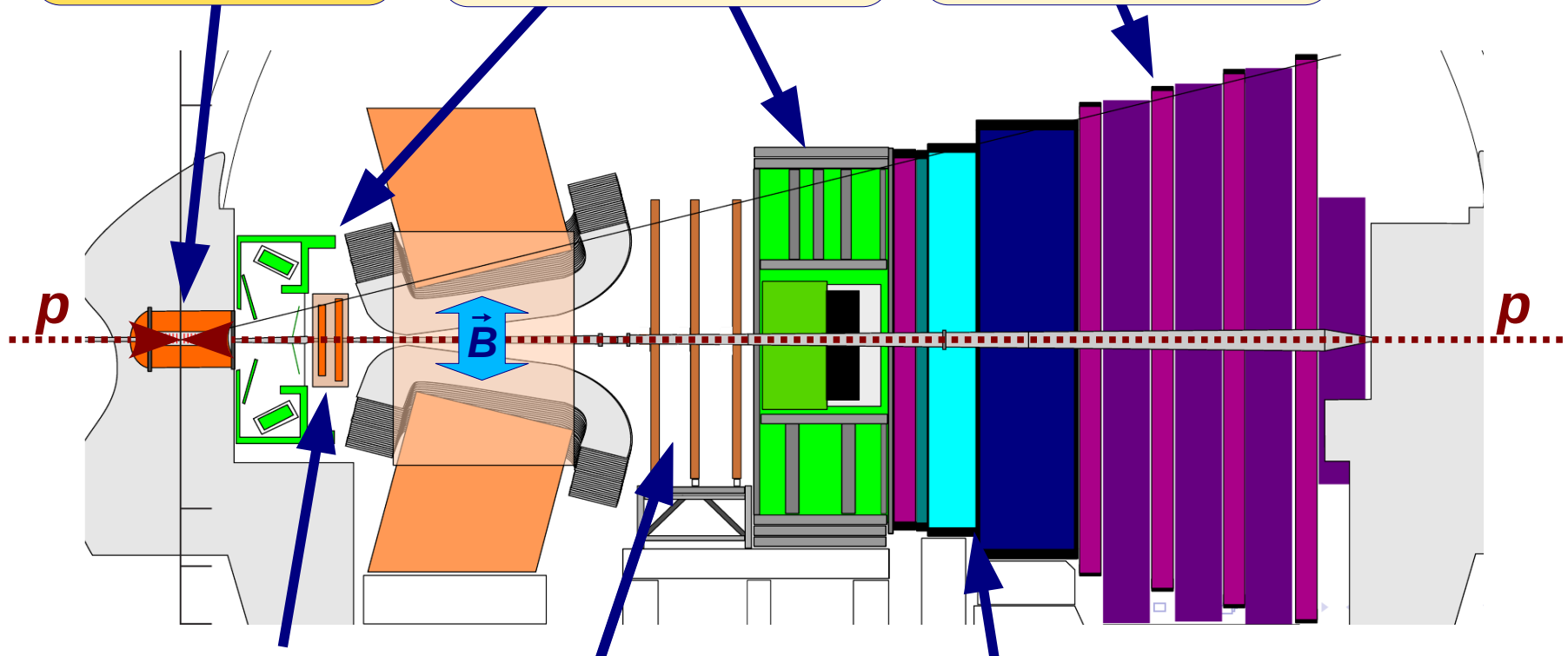
[arXiv:1808.08865]

Upgrade I (2021 ++)

Vertex locator
(silicon pixels)

New optics,
photon detectors

New electronics

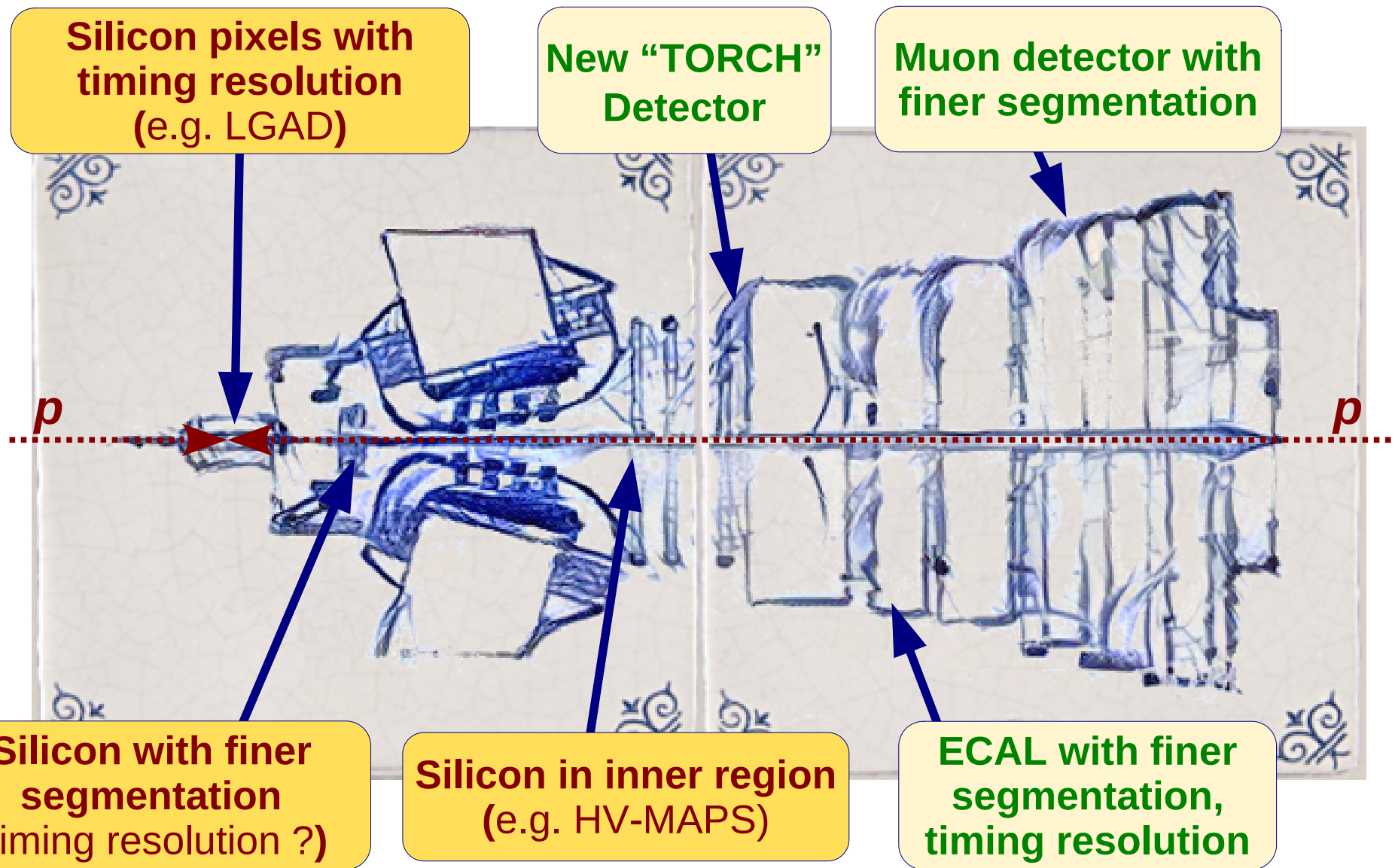


Upstream Tracker
(silicon strips)

Scintillating
Fibre Tracker

New electronics

Upgrade II (2030 ++)

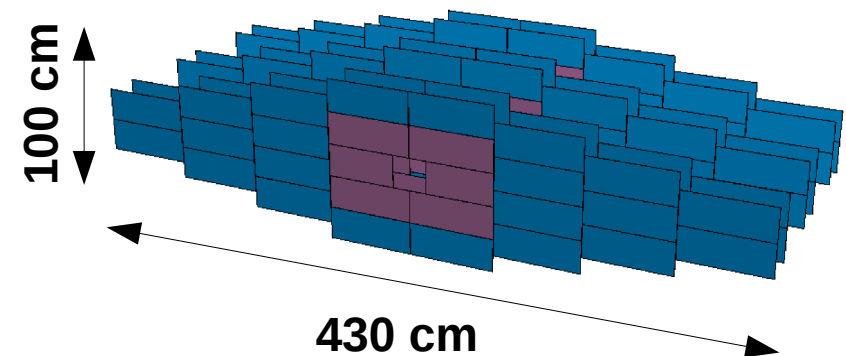
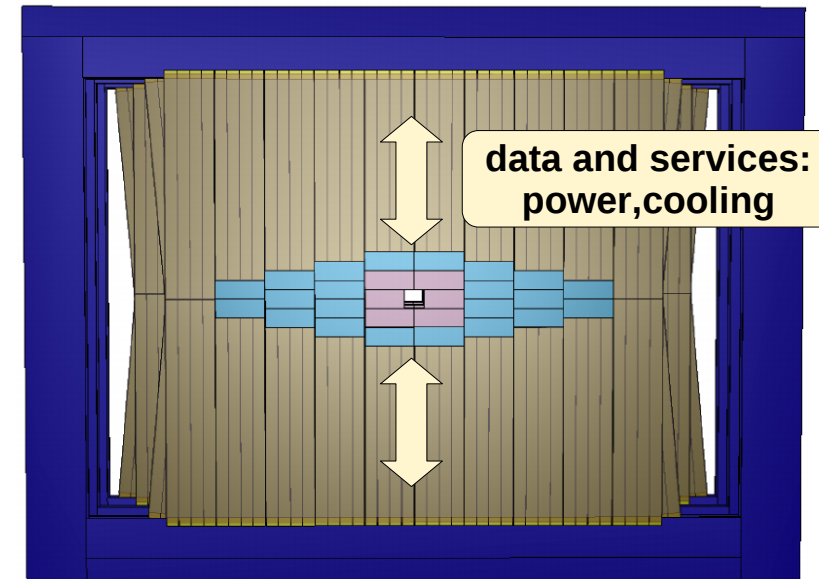


Upgrade II (2030 ++)

Promising technology for inner part:

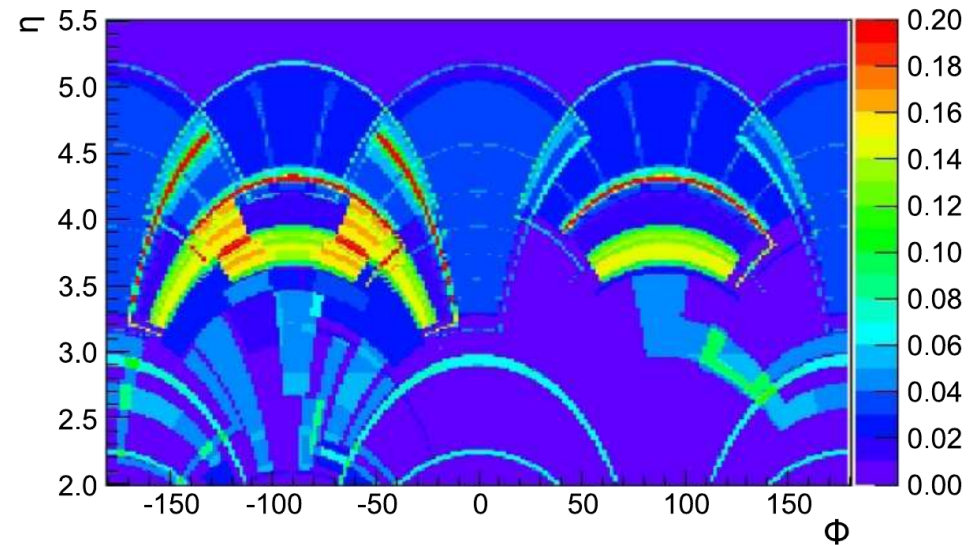
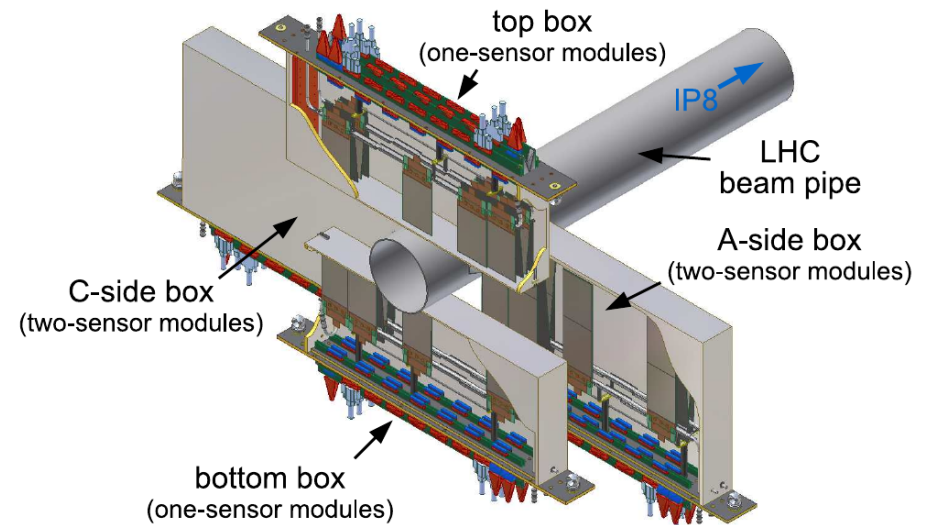
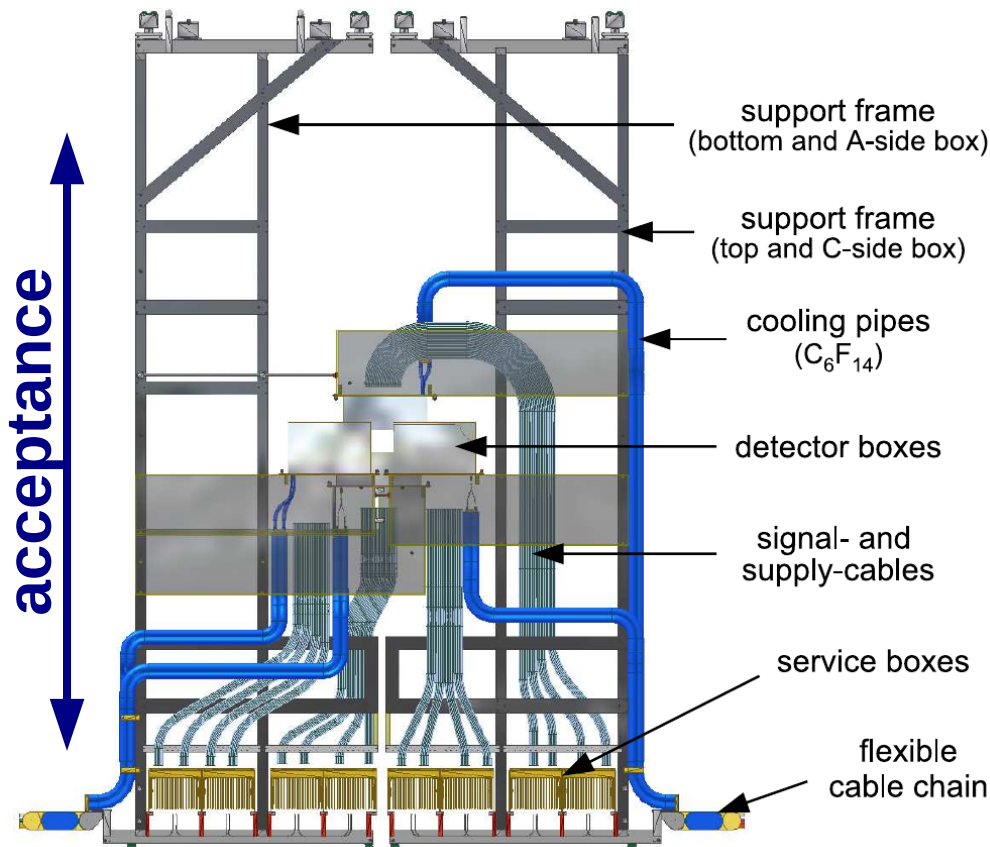
HV-CMOS pixel detectors

- pioneered by mu3 experiment
- sufficiently radiation hard
- thin detectors = little material
 - low power consumption
- details of chip design to be adjusted for LHCb needs
 - (pixel size, front-end data processing)
 - minimize dead material from cables, supports etc

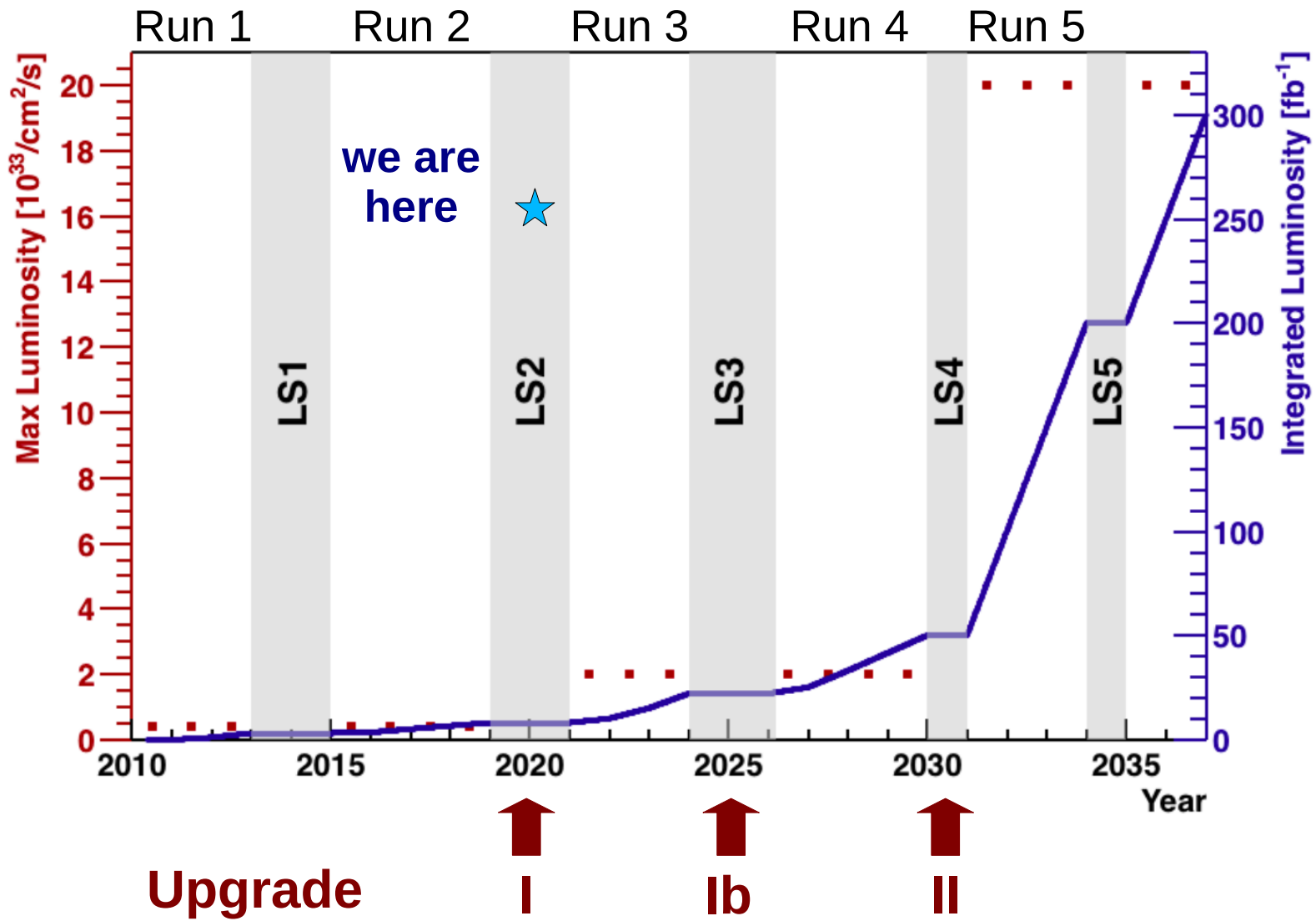


Inner Tracker (2010-2018)

Material completely dominated by supports, cooling, cables



LHCb Upgrades



[arXiv:1808.08865]

Upgrade Ib (≈ 2025)

**Size of the silicon tracker
for Upgrade 2:
keep the occupancy in the
scintillating fibre tracker
at an acceptable level**

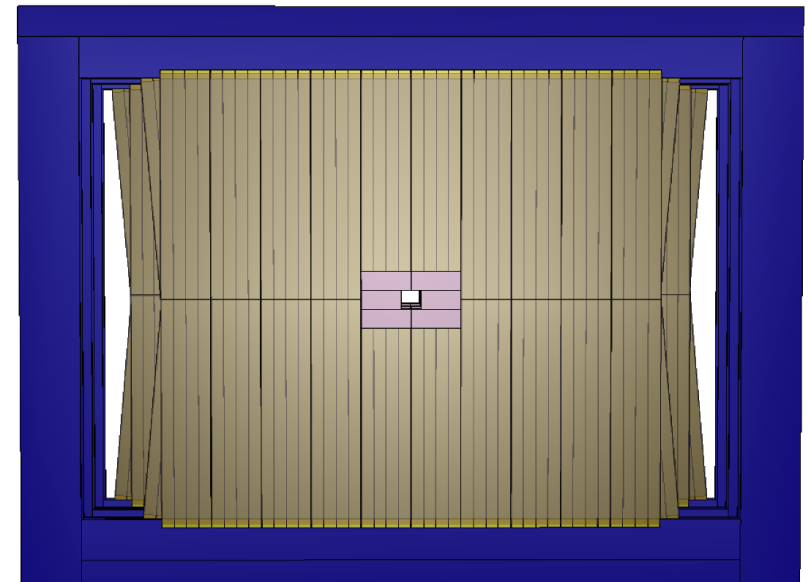
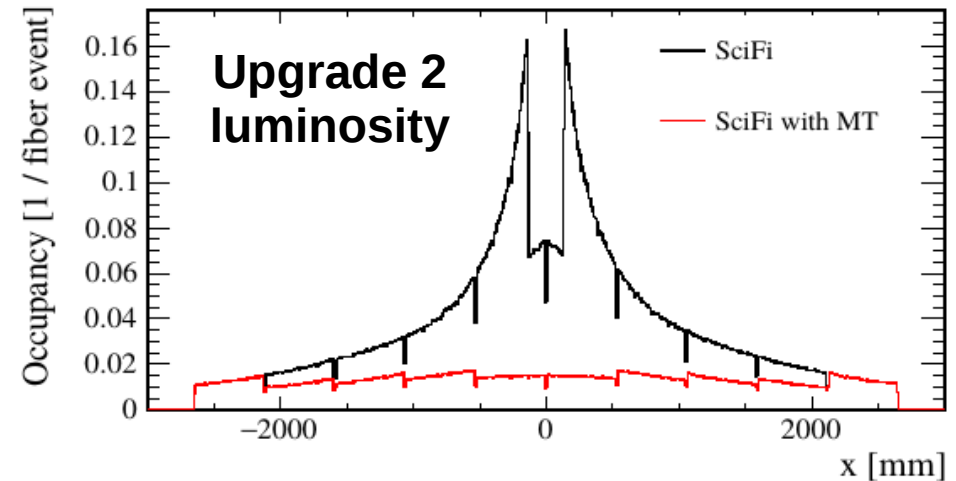
→ 3 m² per layer

→ 18 m² for 6 layers

**Idea: install a smaller version of
the silicon tracker in Upgrade Ib**

→ gain experience with the
new technology

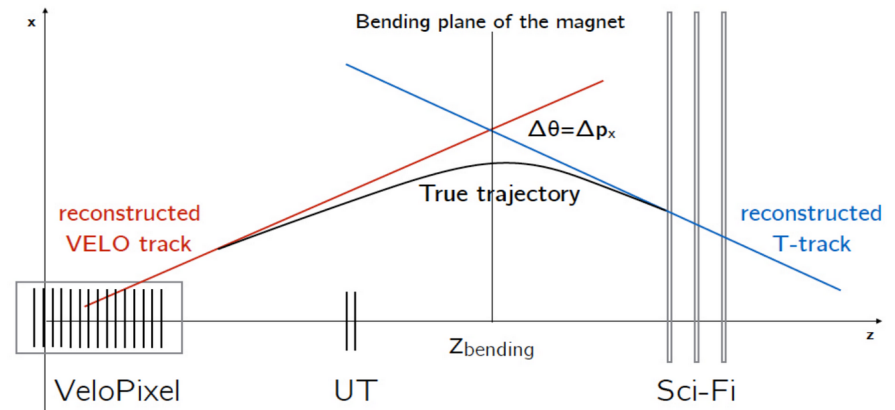
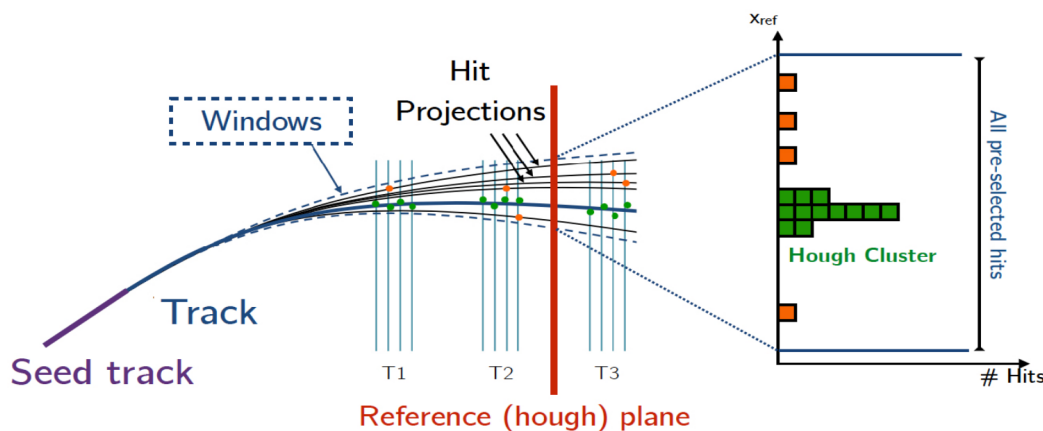
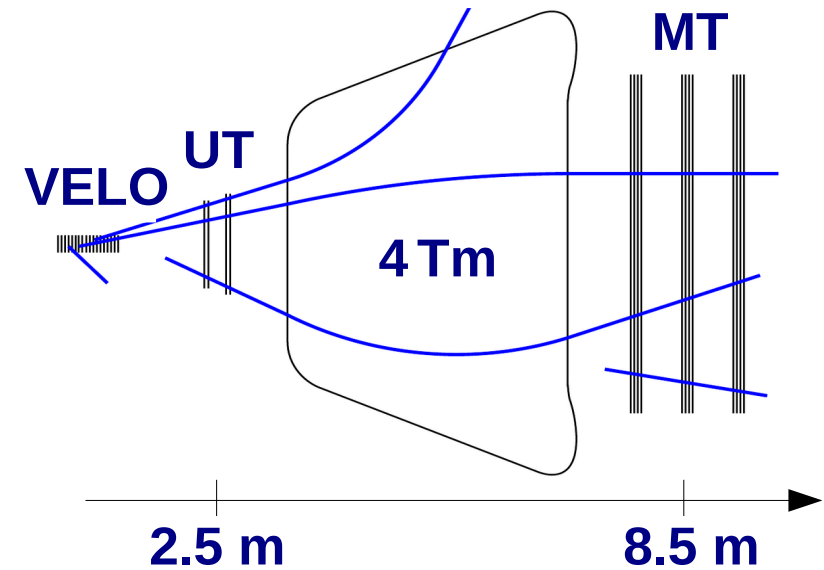
→ improve track reconstruction
performance for LHC Run 4



Track Reconstruction

Expect biggest challenge to be matching between VELO/UT and MT

- Upgrade 2: 2500 charged particles inside LHCb acceptance
- need to extrapolate trajectories over 6 m through magnetic field, without any intermediate information



Summary

Efficient and precise tracking of charged particles is a crucial ingredient for almost all particle physics experiments

- to determine production and decay vertices
- to measure momenta

Detection based on interaction of particle with detector material, e.g.

- ionisation of a gas
- creation of electron/pair holes in a semiconductor

Apply electric field across detector volume, read out the signals induced by drifting charges on segmented electrodes

- wires, strips, pixels

Many (sometimes conflicting) performance requirements

- granularity, spatial resolution, rate capability, radiation hardness, material budget, cost

New detector technologies to face new challenges

Summary

**Did not talk about many, many very interesting things
e.g. use of scintillating fibres for tracking**

e.g. Scintillators and scintillating fibres
play an important role in calorimetry,
I suspect this will be discussed in the lecture
by Giovanni de Lellis on 8th of April

The slides of this lecture are available at

http://www.physik.uzh.ch/~olafs/pdf/200318_MISIS.pdf

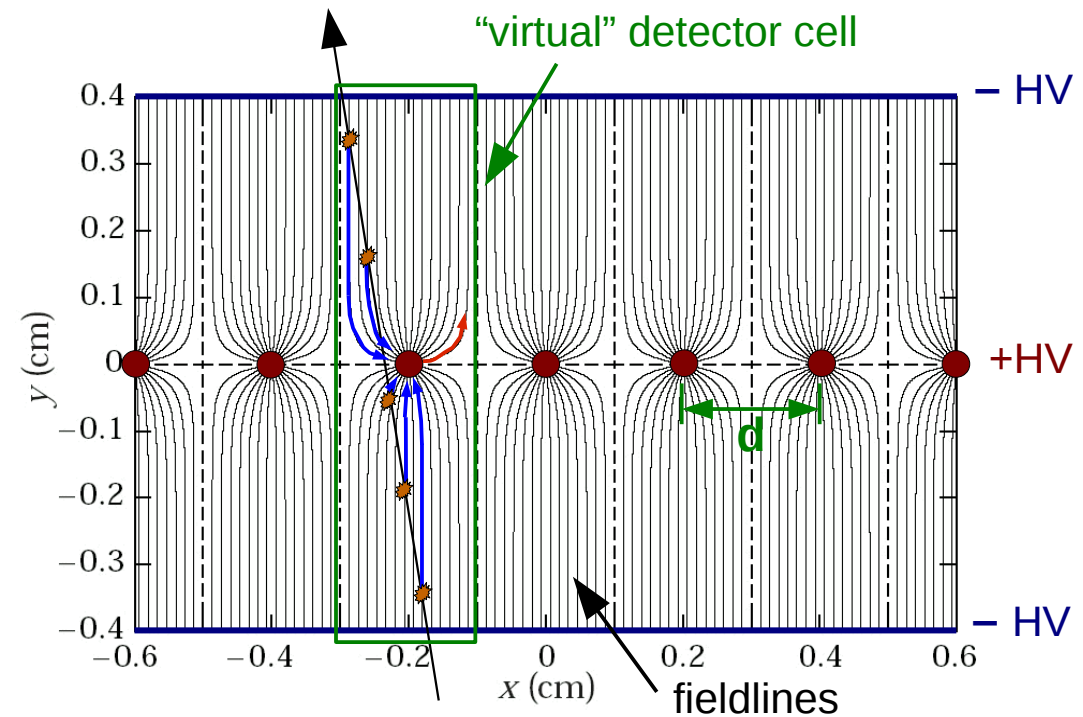
Multi Wire Proportional Chamber

Array of signal wires in between two planar cathodes (Charpak, 1968)

- each wire connected to a readout amplifier and a discriminator
- register a “hit” if signal on the wire is above discriminator threshold
- “binary readout” (hit or no hit)
- spatial resolution given by distance d between wires

$$\sigma \approx d / \sqrt{12}$$

- typically $d \approx 2 \text{ mm} \Rightarrow \sigma \approx 600 \text{ }\mu\text{m}$



- **rate capability up to 10^6 /s**